

DEPARTMENT OF STATISTICS AND DEMOGRAPHY

MAIN EXAMINATION, 2016/17

COURSE TITLE: DESIGN AND ANALYSIS OF EXPERIMENTS

COURSE CODE: ST 404

TIME ALLOWED: THREE (3) HOURS

INSTRUCTION: 1. ANSWER QUESTION ONE AND ANY THREE QUESTIONS;

2. EACH QUESTION CARRIES 25 MARKS.

SPECIAL REQUIREMENTS: SCIENTIFIC CALCULATORS AND STATISTICAL TABLES

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Question 1

The data that follow are observations collected from an experiment that was compared four treatments, A, B, C, and D, within each of three blocks, using a randomized complete-block design.

Block	Treatment				Total
	A	B	C	D	
1	6	10	8	9	33
2	4	9	5	7	25
3	12	15	14	14	55
Total	22	34	27	30	113

- (a) Do the data present sufficient evidence to indicate differences among the treatment means? Test using $\alpha = 0.05$ (10 marks)
- (b) Do the data present sufficient evidence to indicate differences among the block means? Test using $\alpha = 0.05$ (3 marks)
- (c) Perform paired comparisons using Tukey's test with $\alpha = 0.05$ (6 marks)
- (d) Find a 95% confidence interval for the difference in means for treatments A and B. (4 marks)
- (e) Does it appear that the use of a randomized block design for this experiment was justified? Explain. (2 marks)

Question 2

A study was conducted to assess cardiorespiratory fitness level among youth aged 12 to 19 years. Estimated maximum oxygen uptake ($VO_{2\max}$) was used to measure a person's cardiorespiratory level. The focus of the study investigated the relationship between levels of physical activity (more than others, same as others, or less than others) and gender on $VO_{2\max}$. The data that follows are based on this study.

	Physical Activity		
	More	Same	Less
Males	50.1	45.7	40.9
	47.2	44.2	41.3
	49.7	46.8	39.2
	50.4	44.9	40.9
Females	41.2	37.2	36.5
	39.8	39.4	35.0
	41.5	38.6	37.2
	38.2	37.8	35.4

- (a) Is this a factorial experiment or a randomized block design? Explain
- (b) Is there a significant interaction between levels of physical activity and gender? Are there significant differences between males and females? Levels of physical activity? (25 marks)

Question 3**Page 3 of 4**

A study was conducted to determine whether or not there is a significant difference in the amount of aluminium achieved in the analysis between certain levels of certain processing variables. The variables and data are given below:

- A: mixing time level 1 – 2 hours
 level 2 – 4 hours
- B: blade speed level 1 – 36 rpm
 level 2 – 78 rpm
- C: condition of nitrogen passed over propellant
 level 1 – dry
 level 2 – 72% relative humidity
- D: physical state of propellant
 level 1 – uncured
 level 2 – cured

Observation	Physical State	Mixing time	Blade speed	Nitrogen condition	Aluminium
1	1	1	2	2	16.3
2	1	2	2	2	16.0
3	1	1	1	1	16.2
4	1	2	1	2	16.1
5	1	1	1	2	16.0
6	1	2	1	1	16.0
7	1	2	2	1	15.5
8	1	1	2	1	15.9
9	2	1	2	2	16.7
10	2	2	2	2	16.1
11	2	1	1	1	16.3
12	2	2	1	2	15.8
13	2	1	1	2	15.9
14	2	2	1	1	15.9
15	2	2	2	1	15.6
16	2	1	2	1	15.8

The data in the table were recorded. Assuming all two-, three-and four-factor interactions to be negligible, estimate all the main effects and interpret the results. **(25 marks)**

Question 4**Page 4 of 4**

- (a) A router is used to cut locating notches on a printed circuit board. The vibration level at the surface of the board as it is cut is considered to be a source of dimensional variation in the notches. Two factors are thought to influence vibration: bit size (A) and cutting speed (B). Two bit sizes (1/16 and 1/8 inch) and two speeds (40 and 90 rpm) are selected, and four boards are cut at each set of conditions shown below. The response variable is vibration measured as the resultant vector of three accelerometers (x, y and z) on each test circuit board.

A	B	treatment combination	Replicate			
			I	II	III	IV
-	-	(1)	18.2	18.9	12.9	14.4
+	-	a	27.2	24.0	22.4	22.5
-	+	b	15.9	14.5	15.1	14.2
+	+	ab	41.0	43.9	36.3	39.9

Analyse the data from this experiment and draw conclusions on both the main and interaction effects. Use 5% level of significance. **(25 marks)**

Question 5

- (a) Divide the treatment combinations of a 2^4 factorial experiment into four blocks by confounding ABC and BCD. What additional effect is also confounded with blocks? **(12 marks)**

(b) Consider a 2^5 experiment where the experimental runs are on 4 different machines. Use the machines as blocks, and assume that all main effects and two-factor interactions may be important.

- (i) Which runs would be made on each of the 4 machines?
(ii) Which effects are confounded with blocks?

(13 marks)**END OF EXAM!!**

