DEPARTMENT OF STATISTICS AND DEMOGRAPHY

MAIN EXAMINATION, 2015/16

COURSE TITLE:	OPERATIONS RESEARCH II
COURSE CODE:	ST 408
TIME ALLOWED:	THREE (3) HOURS
INSTRUCTION:	ANSWER A TOTAL OF FOUR QUESTIONS SECTION A: ANSWER BOTH QUESTIONS SECTION B: ANY TWO QUESTIONS ALL QUESTIONS CARRY EQUAL MARKS (25 MARKS)
SPECIAL REQUIREMENTS:	SCIENTIFIC CALCULATORS AND STATISTICAL TABLES

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SECTION A

Question 1

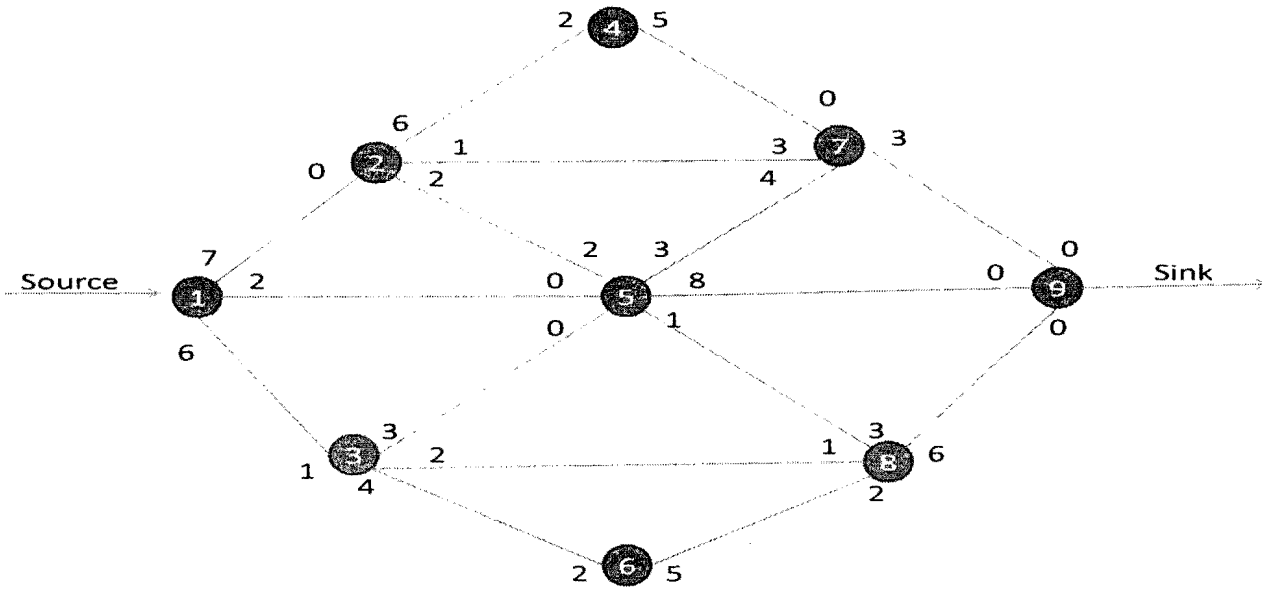
Monica has enjoyed sailing small boats since she was 7 years old when her mother started sailing with her. Today, Monica is considering the possibility of starting a company to produce high quality and stable small sailing boats for the recreational market specifically for children aged 10 and 15 years. She needs to decide on whether to build a large manufacturing facility, small manufacturing facility or no facility at all. With a favourable market, Monica can expect to make $90,000 from a large facility or $60,000 from a small facility. If the market is unfavourable, however, Monica estimates that she will loose $30,000 with a large facility and loose only $20,000 with a small facility. Based on the expense involved in developing initial molds and acquiring the necessary equipment to produce fibreglass sailboats for children, Monica has decided to conduct a pilot study to make sure that the market for the sailboats will be adequate. She estimates that this study will cost $10,000. Furthermore, the pilot study can either be favourable or unfavourable. She estimates that the probability of an favourable market given favourable pilot study is 0.8. The probability of an unfavourable market given unfavourable pilot study to be 0.9. Monica feels that there is a 0.65 chance that the pilot study will be favourable. If Monica bypasses the pilot study, and simply decides to build small, large or no facility, she estimates that the probability of a favourable market is 0.6. What do you recommend? Compute EVSI.

(25 marks)

Question 2

For the following electrical transmission network, find the maximum energy flow from the source to sink.

(25 marks)

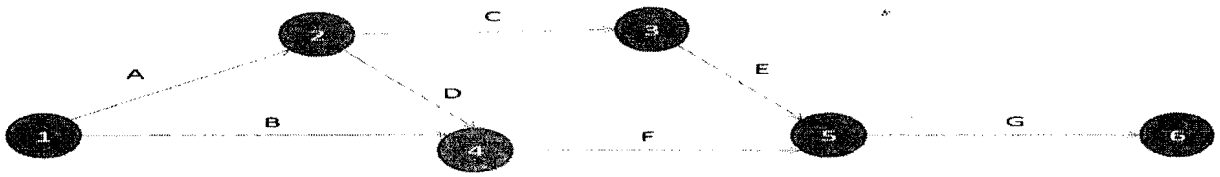


SECTION B

Question 3

The following data relate to a project network shown below:

Activity	Optimistic Time Days	Most likely Time Days	Pessimistic Time Days
A	4	6	8
B	5	9	11
C	6	9	12
D	4	9	9
E	5	7	12
F	7	7	9
G	4	7	10



Determine the following:

(a) The expected activity time and variance of the expected activity time for each activity.
(b) The ES, LS, EF and LF values for each activity.
(c) The slack for each activity.
(d) The critical path for the project
(e) The probability that the project will be completed in 35 days or less
(f) The probability that the project will require 30 or more days to complete.

(10+5+5+1+2+2 marks)

Question 4

(a) Two telephone companies Easy Pay and Budget are competing. A statistical study has shown that in each 6 month period, 60% of the clients of Easypay stay with the company while 40% of them which to Budget. During the same period, 20% of the clients of Budget switch to Easypay, while 80% stay with Budget. On January 1, 2009, Easypay had 50 thousand clients and Budget had 25 thousand clients.

(i) Write the migration matrix M.
(ii) How many clients will each company have on July 1, 2009?
(iii) How many clients will each company have on January 1, 2010?
(iv) Assuming the migration matrix M stays constant in the long term, and the market share (i.e. percentage of the total customers) of each company in the long term. That is, find the equilibrium market shares. **(2+3+3+10 marks)**

(b) Assume that a man's profession can be classified as professional, skilled labourer, or unskilled labourer. Assume that, of the sons of professional men, 80 percent are professional, 10 percent are skilled labourers, and 10 percent are unskilled labourers. In the case of sons of skilled labourers, 60 percent are skilled labourers, 20 percent are professional, and 20 percent are unskilled. Finally, in the case of unskilled labourers, 50 percent of the sons are unskilled labourers, and 25 percent each are in the other two categories. Assume that every man has at least one son, and form a Markov chain by following the profession of a randomly chosen son of a given family through several generations. Set up the matrix of transition probabilities.
Find the probability that a randomly chosen grandson of an unskilled labourer is a professional man.
(7 marks)

Question 5

(a) Dixies Corporation is both a producer and a user of brass couplings. The firm operates 220 days a year and uses couplings at a steady rate of 50 per day. Couplings can be produced at a rate of 200 per day. Annual storage cost is $2 per coupling, and machine setup cost is $70 per run.

(i) Determine the economic run quantity.

(ii) Approximately how many runs per year will be there?

(iii) Compute the maximum inventory level.

(iv) Determine the length of the pure consumption portion of the cycle. **(4+3+3+5 marks)**

(a) The Wet Elbow Paint Shop sells an average of 400 gallons of paint during lead time. The standard deviation of demand during lead time is 50 gallons. The paint market is very competitive, so the store requires a 90 percent service level.

(i) What reorder point should be used to maintain this service level?

(ii) Determine the safety stock level and reorder point if no more than one out of five orders should result in a stock out. **(5 + 5 marks)**

END OF EXAM!!

Standard Normal Probabilities

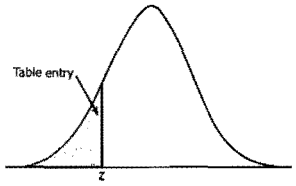


Table entry for z is the area under the standard normal curve to the left of z.

z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
−3.4	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0002
−3.3	.0005	.0005	.0005	.0004	.0004	.0004	.0004	.0004	.0004	.0003
−3.2	.0007	.0007	.0006	.0006	.0006	.0006	.0006	.0005	.0005	.0005
−3.1	.0010	.0009	.0009	.0009	.0008	.0008	.0008	.0008	.0007	.0007
−3.0	.0013	.0013	.0013	.0012	.0012	.0011	.0011	.0011	.0010	.0010
−2.9	.0019	.0018	.0018	.0017	.0016	.0016	.0015	.0015	.0014	.0014
−2.8	.0026	.0025	.0024	.0023	.0023	.0022	.0021	.0021	.0020	.0019
−2.7	.0035	.0034	.0033	.0032	.0031	.0030	.0029	.0028	.0027	.0026
−2.6	.0047	.0045	.0044	.0043	.0041	.0040	.0039	.0038	.0037	.0036
−2.5	.0062	.0060	.0059	.0057	.0055	.0054	.0052	.0051	.0049	.0048
−2.4	.0082	.0080	.0078	.0075	.0073	.0071	.0069	.0068	.0066	.0064
−2.3	.0107	.0104	.0102	.0099	.0096	.0094	.0091	.0089	.0087	.0084
−2.2	.0139	.0136	.0132	.0129	.0125	.0122	.0119	.0116	.0113	.0110
−2.1	.0179	.0174	.0170	.0166	.0162	.0158	.0154	.0150	.0146	.0143
−2.0	.0228	.0222	.0217	.0212	.0207	.0202	.0197	.0192	.0188	.0183
−1.9	.0287	.0281	.0274	.0268	.0262	.0256	.0250	.0244	.0239	.0233
−1.8	.0359	.0351	.0344	.0336	.0329	.0322	.0314	.0307	.0301	.0294
−1.7	.0446	.0436	.0427	.0418	.0409	.0401	.0392	.0384	.0375	.0367
−1.6	.0548	.0537	.0526	.0516	.0505	.0495	.0485	.0475	.0465	.0455
−1.5	.0668	.0655	.0643	.0630	.0618	.0606	.0594	.0582	.0571	.0559
−1.4	.0808	.0793	.0778	.0764	.0749	.0735	.0721	.0708	.0694	.0681
−1.3	.0968	.0951	.0934	.0918	.0901	.0885	.0869	.0853	.0838	.0823
−1.2	.1151	.1131	.1112	.1093	.1075	.1056	.1038	.1020	.1003	.0985
−1.1	.1357	.1335	.1314	.1292	.1271	.1251	.1230	.1210	.1190	.1170
−1.0	.1587	.1562	.1539	.1515	.1492	.1469	.1446	.1423	.1401	.1379
−0.9	.1841	.1814	.1788	.1762	.1736	.1711	.1685	.1660	.1635	.1611
−0.8	.2119	.2090	.2061	.2033	.2005	.1977	.1949	.1922	.1894	.1867
−0.7	.2420	.2389	.2358	.2327	.2296	.2266	.2236	.2206	.2177	.2148
−0.6	.2743	.2709	.2676	.2643	.2611	.2578	.2546	.2514	.2483	.2451
−0.5	.3085	.3050	.3015	.2981	.2946	.2912	.2877	.2843	.2810	.2776
−0.4	.3446	.3409	.3372	.3336	.3300	.3264	.3228	.3192	.3156	.3121
−0.3	.3821	.3783	.3745	.3707	.3669	.3632	.3594	.3557	.3520	.3483
−0.2	.4207	.4168	.4129	.4090	.4052	.4013	.3974	.3936	.3897	.3859
−0.1	.4602	.4562	.4522	.4483	.4443	.4404	.4364	.4325	.4286	.4247
−0.0	.5000	.4960	.4920	.4880	.4840	.4801	.4761	.4721	.4681	.4641

Standard Normal Probabilities

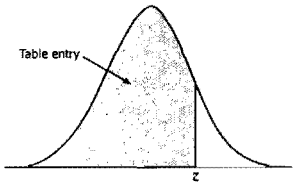


Table entry for z is the area under the standard normal curve to the left of z.

z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359
0.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753
0.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141
0.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517
0.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879
0.5	.6915	.6950	.6985	.7019	.7054	.7088	.7123	.7157	.7190	.7224
0.6	.7257	.7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549
0.7	.7580	.7611	.7642	.7673	.7704	.7734	.7764	.7794	.7823	.7852
0.8	.7881	.7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133
0.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.8790	.8810	.8830
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9279	.9292	.9306	.9319
1.5	.9332	.9345	.9357	.9370	.9382	.9394	.9406	.9418	.9429	.9441
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9686	.9693	.9699	.9706
1.9	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	.9761	.9767
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9916
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936
2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	.9951	.9952
2.6	.9953	.9955	.9956	.9957	.9959	.9960	.9961	.9962	.9963	.9964
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	.9973	.9974
2.8	.9974	.9975	.9976	.9977	.9977	.9978	.9979	.9979	.9980	.9981
2.9	.9981	.9982	.9982	.9983	.9984	.9984	.9985	.9985	.9986	.9986
3.0	.9987	.9987	.9987	.9988	.9988	.9989	.9989	.9989	.9990	.9990
3.1	.9990	.9991	.9991	.9991	.9992	.9992	.9992	.9992	.9993	.9993
3.2	.9993	.9993	.9994	.9994	.9994	.9994	.9994	.9995	.9995	.9995
3.3	.9995	.9995	.9995	.9996	.9996	.9996	.9996	.9996	.9996	.9997
3.4	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9998