

**UNIVERSITY OF SWAZILAND**

**MAIN EXAMINATION 2011**

**TITLE OF PAPER: INDIRECT TECHNIQUES FOR DEMOGRAPHIC ESTIMATION**

**COURSE NUMBER: DEM 303**

**TIME ALLOWED: 3 HOURS**

**INSTRUCTIONS: ANSWER QUESTION 1 AND 2 AND ANY TWO QUESTIONS FROM SECTION B. ALL QUESTIONS ARE WORTH 25 MARKS EACH.**

**REQUIREMENTS: CALCULATOR**

**THIS PAPER SHOULD NOT BE OPENED UNTIL PERMISSION HAS BEEN GIVEN BY THE INVIGILATOR**

## **SECTION A**

### **Question 1**

- a) What is meant by a demographic model? Give three uses of demographic models(8)
- b) Describe briefly the characteristics of each region (family) of the Coale and Demeny regional model life tables. (12)
- c) Discuss the importance of indirect estimation in demography. Elaborate your answer with an example. (5)

### **Question 2**

As a demographer in a government office, you are given the following data for country X:

- i. Children ever born by 5 year age group of mother
- ii. Births in the last year by age of mother
- iii. Children ever born by duration of marriage of mother
- iv. Number of ever married women in each age group
- v. Total number of women in each age group

You are required to calculate the TFR from these data. Describe each of the methods you would use, clearly stating the strengths and weaknesses of each method. (25)

## **SECTION B**

### **Question 3**

The Brass Relational Gompertz model is given as:

$$Y(x) = \alpha + \beta Y^*(x)$$

Where  $Y(x)$  is a Gompit function defined as:  $-\ln [-\ln(F(x))]$  and  $Y^*(x)$  is the standard gompits.

- a) Explain the meanings of  $\alpha$  and  $\beta$ . (4)
- b) Calculate the parameters of the Relational Gompertz model. (16)

Age group	ASFR	$Y^*(x)$
15-19	0.2004	-0.69130
20-24	0.3373	-0.02564
25-29	0.3109	-0.70000
30-34	0.2615	1.47872
35-39	0.1970	2.62602
40-44	0.0954	4.80970
45-49	0.0135	-----

- c) You are given the following parameters for the Brass logit model:  $\alpha = -0.183$  and  $\beta = 0.928$ . Calculate the value for  $l_{45}$  given that  $\lambda(l_{45}) = -0.1073$ . (5)

#### Question 4

- a) What is meant by a stable population? (3)
- b) Using the data in Table 1 below calculate the intrinsic rate of natural increase .(8)

**Table 1: Data for Calculation of intrinsic rate of natural increase**

Age Group	Female ASFRs per woman	Probability of survival
15-19	0.01289	0.98615
20-24	0.05007	0.98376
25-29	0.07120	0.98134
30-34	0.03947	0.97877
35-39	0.01205	0.97530
40-44	0.00215	0.96960
45-49	0.00012	0.96003

- c) Two types of demographic models are of particular importance. Give a brief description of the two types.(4)
- d) What is the probability of a male surviving to age 5 in a population whose probability of surviving to age 2 is 0.84? Assume the pattern of mortality resembles that of the CD North model life table.(5)
- e) Find the value of  $4q_1$  corresponding to level 12.8 in the female West model life table.(5)

#### Question 5

- a) What are the assumptions for the orphanhood method for estimating adult mortality? (6)
- b) Using the the Brass maternal orphanhood method, calculate the probability of survival from age 20 to age 45 and from age 20 to 50. Assume that  $M= 26.75$  years. (8)

Age group	Proportion with mother alive S(n)
20-24	0.9050
25-29	0.8513
30-34	0.7805
35-39	0.6923

You may find the following information useful:

Mean age, M			
n	25	26	27
20	0.673	0.756	0.838
25	0.704	0.809	0.913
30	0.708	0.834	0.957

- c) What are the assumptions for the method for estimating adult mortality using intercensal survivorship probabilities? (6)
- d) What are the limitations of this method? (5)

### Question 6

- a) What are the assumptions of the Brass method for estimating childhood morality using information from women on the proportion of children dead? (5)
- b) You are given the data below on average parity per woman and proportion of children dead classified by age group of women. Using Trussel's variant of the Brass method, calculate q(2) and q(3). (10)

Age group	i	Average parity	Proportion dead
15-19	1	0.156	0.0959
20-24	2	1.326	0.1218
25-29	3	2.765	0.1485

You may find the following information useful:

i	a(i)	b(i)	c(i)
1	1.0819	-3.0005	0.8689
2	1.2846	-0.6181	-0.3024
3	1.2223	0.0851	-0.4704

- c) Describe the Preceding Birth technique for indirect estimation of childhood mortality. Make sure to include the advantages and limitations for this method.(10)

TABLE XIV. Values of  $l_x$  by single years of age from 1 to 5 for regional model life tables ( $t_0 = 100,000$ ) at mortality levels 1-24

M O D E L									
W E S T					N O R T H				
L E V E L	Females				Males				$l_4$
	$l_1$	$l_2$	$l_3$	$l_4$	$l_1$	$l_2$	$l_3$	$l_4$	
1	63445	51958	51154	48696	46836	58050	50262	46851	44617
2	66601	58514	52549	52549	50776	61614	54105	48663	42957
3	69444	61785	58353	56135	54456	64826	57643	54917	4062
4	72027	64811	61578	59488	57907	67743	60918	54437	50906
5	74389	67625	61152	62634	61152	70411	63965	55972	5517
6	76562	70251	67293	65596	64213	72865	66812	6142	59293
7	78571	72713	70088	68391	67107	75135	69481	64160	61133
8	80438	75028	7204	71037	69852	77243	71992	67004	65382
9	82178	77211	74986	73547	72459	79209	74360	6985	67066
10	83807	79276	77246	75933	74940	81049	76601	72237	69846
11	85336	81233	79394	78206	77307	82775	78726	7430	73378
12	86775	83092	81141	80374	79567	84401	80745	76953	74928
13	88121	84865	8305	82462	81749	85983	82816	79144	77316
14	89396	86646	85413	84616	84013	87487	84756	81428	79844
15	90606	88290	87242	86559	86037	88606	85650	8094	80277
16	91769	89864	88987	88407	87954	90084	88086	87208	86632
17	92884	91352	90635	90153	89772	91322	89716	88976	88098
18	93949	92759	9192	91806	91496	92517	91266	90662	89921
19	94965	94089	93664	93372	93134	93666	92736	92266	91672
20	95931	95347	95059	94859	94693	94767	94129	93791	93353
21	96884	96531	96555	96231	96127	95866	95460	95236	94937
22	97718	97507	97400	97324	97260	96901	96648	96501	96302
23	98470	98361	98305	98264	98230	97838	97699	97616	97499
24	99095	99048	99024	99007	98992	98652	98588	98492	98492
25	99555	99540	99533	99522	99527	99289	99266	99252	99240
M O D E L									
L E V E L	Females				Males				$l_4$
	$l_1$	$l_2$	$l_3$	$l_4$	$l_1$	$l_2$	$l_3$	$l_4$	
1	68005	59681	54557	50689	47753	62858	54755	49828	46166
2	70776	62905	58061	54403	51626	66052	5313	5306	43381
3	73263	65852	61290	57847	55232	68952	61570	57101	47449
4	75516	68564	64285	61055	56602	71515	64572	53780	51254
5	77570	71074	67074	64055	61763	73883	63550	57212	51826
6	79456	73407	69683	66871	64737	76057	69943	6382	58187
7	81196	75585	72130	69523	67543	78062	72362	68895	64360
8	82808	77625	7434	72025	70197	79920	74631	69023	66319
9	84308	79542	76608	74394	72712	81650	76764	73793	71586
10	85709	81349	78665	76639	75101	83264	78777	76048	74019
11	87022	83056	80615	78772	78373	84777	80679	78187	74247
12	88253	84670	82464	80779	79535	86196	82479	80218	77261
13	89398	86244	84302	82837	81724	87529	84250	80767	79638
14	90441	87729	86046	84770	83796	88709	85835	84087	81801
15	91453	89164	87717	86609	85751	89858	87367	85852	83870
16	92431	90521	89291	88340	86595	90975	88909	87598	86608
17	93372	91802	90773	89971	89335	92054	90376	89258	88399
18	94274	93012	92170	90508	90978	93094	91759	90827	89526
19	95136	94153	93487	9259	92531	94091	93061	92309	91712
20	95956	95230	9429	91330	91003	95043	94286	92706	92866
21	96736	96246	95904	95628	95601	95950	95437	95026	94420
22	97487	97221	97032	96819	96753	96826	96534	96290	96089
23	98122	97974	97867	97780	97708	97580	97408	97028	97134
24	98723	98648	98593	98510	98320	9830	98148	98022	98022
25	99219	99187	99163	99144	99127	98944	98904	98834	98834

TABLE XIV (Continued). Values of  $l_x$  by single years of age from 1 to 5 for regional model life tables ( $l_0 = 100,000$ ) at mortality levels 1 to 24

LEVEL	$l_1$	M O D E L				E A S T				M O D E L				S O U T H				
		$l_2$	$l_3$	$l_4$	$l_5$	$l_1$	$l_2$	$l_3$	$l_4$	$l_1$	$l_2$	$l_3$	$l_4$	$l_1$	$l_2$	$l_3$		
1	57180	49795	46656	44596	43167	49453	42922	40206	38482	37222	42680	42680	42680	41436	41436	41436	41436	
2	60636	53494	50458	48466	47084	53511	47063	44382	42680	46644	48305	46644	46644	45431	45431	45431	45431	
3	63188	56935	54022	52111	50784	57211	50920	52003	50399	54530	52003	50399	50399	49227	49227	49227	49227	
4	66680	60150	57375	55554	54290	60606	54530	57920	55500	53963	53963	53963	53963	52840	52840	52840	52840	
5	69350	63168	60540	58815	57619	63741	66649	61115	57353	61963	60584	61963	60584	56286	56286	56286	56286	
6	71827	66009	63536	61913	60786	66649	66649	61115	59577	61963	60584	61963	60584	59577	59577	59577	59577	
7	74135	68692	66378	64880	63806	69358	64135	61115	59577	63670	62725	63670	62725	62725	62725	62725	62725	
8	76292	71232	69081	67670	66690	71891	66997	64962	62725	66620	65742	66620	65742	65742	65742	65742	65742	
9	78317	73643	71657	70353	69448	74268	69715	67822	65742	70555	69445	68635	69445	68635	68635	68635	68635	
10	80221	75936	74115	72920	72090	76504	72303	70555	68635	72304	71520	72304	71520	71520	71520	71520	71520	
11	82003	78166	76535	75464	74722	78599	74819	73247	71520	77249	74850	77249	74850	74850	74850	74850	74850	
12	83663	80270	78828	77881	77225	80159	77144	75741	74850	77357	74850	77357	74850	74850	74850	74850	74850	
13	85760	82285	81020	80191	79615	82373	79387	76781	74850	79770	76781	79770	76781	76781	76781	76781	76781	
14	86794	84213	83117	82397	81897	84161	81547	80461	79770	81657	80292	81657	80292	81657	81657	81657	81657	
15	88267	86059	85059	84077	83626	85054	84077	82688	81657	83626	82688	83626	82688	83626	83626	83626	83626	
16	89677	87823	87035	86518	86159	87536	85624	84829	83626	87536	84324	83956	84324	83956	83956	83956	83956	
17	91028	89531	88885	88455	88151	89123	87544	86887	85624	89123	86470	86166	86470	86166	86166	86166	86166	
18	91160	90650	90305	90055	90055	90643	90406	88879	86887	90539	90539	90539	90539	90539	90539	90539	90539	
19	93348	92706	92328	92069	91877	92095	91200	90797	90539	92095	91200	90797	90539	90539	90539	90539	90539	
20	94171	94176	93927	93753	93622	93480	92897	92620	92429	93480	92620	92429	92620	92429	92429	92429	92429	
21	95904	95546	95380	95262	95171	94852	94462	94127	94018	95262	94127	94018	95262	94127	94127	94127	94127	
22	96939	96718	96614	96539	96481	96111	95868	95468	95171	96111	95468	95171	95468	95171	95171	95171	95171	
23	97861	97739	97681	97638	97605	97245	97110	97035	96935	97245	97110	97035	96935	97110	97110	97110	97110	
24	98640	98583	98555	98535	98518	98219	98154	98088	98088	98555	98154	98088	98088	98088	98088	98088	98088	
25	99245	99223	99212	99204	99204	99198	98963	98963	98963	99223	98963	98963	98963	98963	98963	98963	98963	
1	69279	55503	49161	45812	43909	53923	53923	53923	53923	57056	57056	57056	57056	45074	45074	45074	45074	
2	71532	58606	52655	49512	47727	68857	68857	68857	68857	71056	59951	59951	59951	52083	47053	47053	47053	
3	73567	61479	55913	52974	51304	54668	54668	54668	54668	73058	62645	62645	62645	50567	50567	50567	50567	
4	75420	64152	58964	56225	55842	57842	57842	57842	57842	74894	65163	65163	65163	53846	53846	53846	53846	
5	77119	66651	61832	59287	57842	60843	60843	60843	60843	76586	67526	67526	67526	56941	56941	56941	56941	
6	78685	68997	64537	62181	60492	63689	63689	63689	63689	78154	69750	69750	69750	62649	62649	62649	62649	
7	80136	71206	67094	64923	64923	66394	66394	66394	66394	79613	71850	71850	71850	63796	63796	63796	63796	
8	81487	73291	69518	67525	66620	68968	68968	68968	68968	80975	73838	73838	73838	66351	66351	66351	66351	
9	82748	75265	71820	70001	72382	71447	72229	72229	72229	75650	70546	70546	70546	67807	67807	67807	67807	
10	83916	77145	74028	72408	72408	74636	73801	73337	77434	74711	73252	73252	73252	72446	72446	72446	72446	
11	84937	78890	76106	74795	76054	78449	78449	78449	78449	79153	76724	76724	76724	74702	74702	74702	74702	
12	85933	80569	78099	76795	78863	78211	85474	80809	80809	80278	82405	82405	82405	76867	76867	76867	76867	
13	86903	82184	80011	81845	81845	80846	80846	80846	80846	86501	82300	82300	82300	80935	80935	80935	80935	
14	87848	83738	81378	81845	81845	82748	82260	82260	82260	87498	83941	83941	83941	81420	81420	81420	81420	
15	88764	85232	83606	82748	82748	84573	84161	88463	85419	88463	85419	85419	85419	83262	83262	83262	83262	
16	89651	86670	85297	85297	85297	86334	86334	86334	86334	89397	86841	86841	86841	85031	84682	84682	84682	
17	90509	88068	86936	88523	88038	87751	90303	90303	88235	87270	86749	86749	86749	86457	86457	86457	86457	
18	91342	89424	89424	90774	90064	89676	89440	89440	89589	91361	89132	89132	89132	88493	88493	88493	88493	
19	92266	90774	90774	92044	91496	91193	91004	91004	92369	92369	91237	91237	91237	90150	90150	90150	90150	
20	93180	92044	92044	93226	92849	92620	92475	92475	93372	93372	92551	92551	92551	91718	91718	91718	91718	
21	94089	93226	93226	94449	94449	94116	93952	93952	93952	94367	93799	93799	93799	93306	93306	93306	93306	
22	94988	94449	94449	95484	95484	95181	95181	95181	95181	95293	94973	94973	94973	94557	94557	94557	94557	
23	95868	96176	96176	96483	96483	96296	96296	96296	96296	96287	96064	95934	95934	95934	95799	95799	95799	95799
24	96716	97386	97386	97514	97321	97282	97282	97282	97282	97282	97282	97282	97282	96937	96937	96937	96937	