

UNIVERSITY OF SWAZILAND

FINAL EXAMINATION PAPER 2010

TITLE OF PAPER : DESIGN AND ANALYSIS OF EXPERIMENTS

COURSE CODE : ST404

TIME ALLOWED : TWO (2) HOURS

REQUIREMENTS : CALCULATOR AND STATISTICAL TABLES

INSTRUCTIONS : ANSWER ANY THREE QUESTIONS

Question 1

[20 marks, 6+9+5]

- (a) Complete the following ANOVA table for a RCBD, in which each treatment appeared once in each block.

Source	SS	df	MS	F ₀
Treatments	12	?	?	?
Blocks	?	4	6	
Error	36	?	?	
Total	?	19		

- (b) Suppose that you wish to investigate 3 fertilizer types ('A', 'B', 'C'), by applying them to crops in 3 regions of land. There are thought to be two nuisance factors at play - the regions themselves ('R1', 'R2', 'R3') and the farmers (Brown, Smith, and Doe).

- Assuming that these factors do not interact, write down a design which will allow for the estimation of all of their main effects, with only 9 crops being planted.
- In a notation such as is used in class, write down the **effects model** for the data.
- How many degrees of freedom will be associated with SS_E ?

- (c) The following questions require only very short answers:

- Suppose that independent observations Y_1, \dots, Y_n are taken from a population with a mean of zero and a variance of σ^2 . How can these be combined to form a random variable X which has a χ_n^2 distribution? What then is the expected value of X ?
- Explain why, in a fixed effects model which contains an overall mean and various treatment effects, we can always assume that the sum of the treatment effects is zero.
- Suppose that the population of womens heights is normally distributed, with a variance of 1 cm. I am curious as to whether or not the mean height is 165 cm. To test the hypothesis that it is 165 cm. I observe that a certain (randomly selected) women has a height of 166 cm. On the basis of this, how do I compute the p-value associated with my hypothesis?
- We commonly use one of two procedures for making multiple comparisons among mean effects. Which of the two - Least Significant Difference or Tukey's - maintains the experimentwise error rate at a fixed value, regardless of how many comparisons are made?

Question 2

[20 marks, 12+4+4]

- (a) In order to investigate the relative effectiveness of three insecticides, a sample of 30 fields was compiled. One of the insecticides was applied in each of ten fields, and one hour later the abundance of insects was measured.

- What is the name of the design being used here?
- Describe the nature of the randomization which should be used. Are all 30 observations made in a completely random order, or is some other mechanism used?
- Write down the (fixed) effects model describing the abundance. Remember to include any relevant constraints on the parameters.

- (b) Write down a 3×3 Graeco-Latin square.
- (c) Write down the statistical model for a 3×3 Latin square design.

Question 3

[20 marks, 18+2]

- (a) Specimens of milk from a number dairies in three different districts were analyzed, and the concentration of the radioactive isotope *Strontium-90* was measured in each specimen. Suppose that specimens were obtained from four dairies in the first district, for six dairies in the second district, and from three dairies in the third district; and the results measured in *picocuries* per litre were as follows:

District 1: 6.4, 5.8, 6.5, 7.7
 District 2: 7.1, 9.9, 11.2, 10.5, 6.5, 8.8
 District 3: 9.5, 9.0, 12.1

- (i) Test whether the variance of the concentration of *Strontium-90* is the same for the dairies in all three districts. State clearly your null and alternative hypothesis, decision rule and present your conclusions.
- (ii) Test whether the concentration of *Strontium-90* is the same for the dairies in all three districts. State clearly your null and alternative hypothesis, decision rule and present your conclusions.
- (iii) Compute 95% family-wise confidence intervals for the mean difference in concentration between District 1 and 2 and District 1 and 3. Use the most efficient approach.

- (b) Show that

$$E\{MS_E\} = \sigma^2$$

$$\text{NB: } MS_E = \frac{1}{n-a} \sum_i \sum_j (Y_{ij} - \bar{Y}_{i+})^2$$

Question 4

[20 marks, 10+4+6]

- (a) In a study to compare the reflective properties of various paints, three different types of paints were applied to specimens of five different types of plastic surfaces. Suppose the observed results in appropriate coded units were as given in table 1.

Table 1: Paint question

Type of paint	Type of surface				
	1	2	3	4	5
1	14.5	13.6	16.3	23.2	19.4
2	14.6	16.2	14.8	16.8	17.3
3	16.2	14.0	15.5	18.7	21.0

- (i) Assume an ANOVA is appropriate, test whether the reflective properties of the three paints are equivalent. State clearly your null and alternative hypothesis, decision rule and present your conclusions.

- (ii) State the assumptions made in your analysis and briefly, without further calculation, how you would check them.
- (iii) What are the advantages of a randomized complete block design?
- (b) In order to compare automobile repair costs at the 2 repair shops in a certain locale, investigators collect a sample of 12 cars which have been in accidents and need repairs. Each car is taken to both repair shops, and estimates of the repair costs are obtained. In terms of

$$y_{ij} = \text{estimated cost from shop } i \text{ to repair car } j \quad (i = 1, 2, \dots, 12)$$

what is the statistic that should be calculated in order to test the hypothesis that the mean repair costs are the same at the two shops?

- (c) Consider the following linear combinations of interest in a single-factor study involving four factor levels:

$$\mu_1 + 3\mu_2 - 4\mu_3 \quad (1)$$

$$0.3\mu_1 + 0.5\mu_2 + 0.1\mu_3 + 0.1\mu_4 \quad (2)$$

$$\frac{\mu_1 + 3\mu_2 + \mu_3}{3} - \mu_4 \quad (3)$$

- (i) Which of the linear combinations are contrasts? State the coefficients for each of the contrasts.
- (ii) Give an unbiased estimator for each of the linear combinations. Also give the estimated variance of each estimator assuming that $n_i = n$.

Table A.1

Cumulative Standardized Normal Distribution

$A(z)$ is the integral of the standardized normal distribution from $-\infty$ to z (in other words, the area under the curve to the left of z). It gives the probability of a normal random variable not being more than z standard deviations above its mean. Values of z of particular importance:

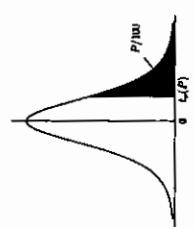
z	$A(z)$	Lower limit of right 5% tail	Lower limit of right 2.5% tail	Lower limit of right 1% tail	Lower limit of right 0.5% tail	Lower limit of right 0.1% tail	Lower limit of right 0.05% tail			
0.0	0.0000	0.5000	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.1398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.2193	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.3179	0.6217	0.6245	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.4354	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.5691	0.6924	0.6958	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7224
0.6	0.7127	0.7291	0.7324	0.7357	0.7422	0.7454	0.7485	0.7517	0.7549	0.7573
0.7	0.7536	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852	0.7879
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8663	0.8685	0.8696	0.8715	0.8729	0.8749	0.8770	0.8790	0.8810
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9101	0.9115	0.9147	0.9162	0.9177	0.9191
1.4	0.9192	0.9202	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9362	0.9373	0.9384	0.9394	0.9405	0.9418	0.9431
1.6	0.9432	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9533	0.9545
1.7	0.9554	0.9564	0.9577	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9785	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817	0.9821
2.1	0.9811	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9851	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9887	0.9890	0.9893
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9958	0.9959	0.9960	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9968	0.9969	0.9970	0.9971	0.9972	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9980	0.9981	0.9982
2.9	0.9981	0.9981	0.9982	0.9983	0.9984	0.9984	0.9985	0.9986	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9988	0.9989	0.9989	0.9990	0.9990
3.1	0.9990	0.9991	0.9991	0.9993	0.9994	0.9994	0.9994	0.9994	0.9995	0.9995
3.2	0.9993	0.9993	0.9994	0.9994	0.9995	0.9995	0.9996	0.9996	0.9996	0.9996
3.3	0.9995	0.9995	0.9995	0.9995	0.9996	0.9996	0.9996	0.9997	0.9997	0.9997
3.4	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997
3.5	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998
3.6	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998

Percentage Points of the t -Distribution

This table gives the percentage points $t_{\alpha}(P)$ for various values of P and degrees of freedom v , as indicated by the figure to the right.

The lower percentage points are given by symmetry as $-t_{\alpha}(P)$, and the probability that $|t| \geq t_{\alpha}(P) = 2P/100$.

The limiting distribution of t as $v \rightarrow \infty$ is the normal distribution with zero mean and unit variance.



v	Percentage points P									
	10	5	2.5	1	0.5	0.1	0.05	0.01	0.001	0.0001
1	3.078	6.314	12.706	31.821	63.657	318.309	636.619			
2	1.476	2.015	2.571	3.365	4.032	5.893	6.869			
3	1.638	2.353	3.182	4.541	5.841	10.215	12.924			
4	1.533	2.132	2.776	3.747	4.604	7.173	8.610			
5	1.476	2.015	2.571	3.365	4.032	5.893	6.869			
6	1.440	1.943	2.447	3.143	3.707	5.208	5.959			
7	1.415	1.865	2.365	2.998	3.498	4.785	5.408			
8	1.397	1.800	2.306	2.891	3.455	4.501	5.041			
9	1.383	1.833	2.262	2.821	3.250	4.297	4.781			
10	1.372	1.812	2.228	2.764	3.169	4.144	4.587			
11	1.363	1.796	2.201	2.718	3.106	4.075	4.437			
12	1.356	1.782	2.179	2.681	3.055	3.930	4.318			
13	1.350	1.771	2.160	2.650	3.012	3.882	4.221			
14	1.345	1.761	2.145	2.624	2.977	3.787	4.140			
15	1.341	1.753	2.131	2.602	2.947	3.733	4.073			
16	1.337	1.746	2.120	2.583	2.921	3.686	4.015			
17	1.330	1.734	2.101	2.552	2.878	3.610	3.922			
18	1.323	1.721	2.080	2.518	2.851	3.577	3.819			
19	1.316	1.708	2.060	2.485	2.787	3.450	3.725			
20	1.310	1.697	2.042	2.457	2.750	3.385	3.646			
21	1.313	1.687	2.021	2.423	2.704	3.307	3.551			
22	1.309	1.676	2.009	2.403	2.678	3.261	3.496			
23	1.304	1.667	1.994	2.381	2.648	3.211	3.435			
24	1.299	1.650	1.984	2.364	2.626	3.174	3.390			
25	1.294	1.637	1.967	2.346	2.600	3.150	3.375			
26	1.290	1.620	1.949	2.326	2.580	3.120	3.350			
27	1.286	1.603	1.930	2.306	2.556	3.090	3.320			
28	1.282	1.586	1.910	2.286	2.531	3.060	3.290			
29	1.278	1.569	1.890	2.266	2.506	3.020	3.260			
30	1.274	1.552	1.870	2.246	2.481	2.990	3.230			
31	1.270	1.535	1.850	2.226	2.456	2.960	3.190			
32	1.266	1.518	1.830	2.206	2.431	2.930	3.160			
33	1.262	1.501	1.810	2.186	2.406	2.900	3.130			
34	1.258	1.484	1.790	2.166	2.381	2.870	3.100			
35	1.254	1.467	1.770	2.146	2.356	2.840	3.070			
36	1.250	1.450	1.750	2.126	2.331	2.810	3.040			
37	1.246	1.433	1.730	2.106	2.306	2.780	3.010			
38	1.242	1.416	1.710	2.086	2.281	2.750	2.980			
39	1.238	1.399	1.690	2.066	2.256	2.720	2.950			
40	1.234	1.382	1.670	2.046	2.231	2.690	2.920			
41	1.230	1.365	1.650	2.026	2.206	2.660	2.890			
42	1.226	1.348	1.630	2.006	2.181	2.630	2.860			
43	1.222	1.331	1.610	1.986	2.156	2.600	2.830			
44	1.218	1.314</								

Percentage Points of the χ^2 -Distribution

This table gives the percentage points $\chi_{\nu}^2(P)$ for various values of P and degrees of freedom ν , as indicated by the figure to the right.
 If X is a variable distributed as χ^2 with ν degrees of freedom, $P/100$ is the probability that $X \geq \chi_{\nu}^2(P)$.
 For $\nu > 100$, $\sqrt{2X}$ is approximately normally distributed with mean $\sqrt{2\nu - 1}$ and unit variance.

ν	10	5	2.5	1	0.5	0.1	0.05	Percentage points P
1	2.706	3.841	5.024	6.635	7.379	10.323	12.116	
2	4.605	5.991	7.378	9.210	10.597	13.816	16.202	
3	6.251	7.815	9.348	11.345	12.838	16.266	17.730	
4	7.779	9.488	11.143	13.277	14.860	18.467	19.987	
5	9.236	11.070	12.833	15.086	16.750	20.515	22.105	
6	10.645	12.592	14.449	16.812	18.548	22.458	24.103	
7	12.017	14.067	16.013	18.475	20.276	24.322	26.018	
8	13.362	15.507	17.535	20.090	21.956	26.124	27.868	
9	14.684	16.919	19.023	21.066	23.589	27.877	29.865	
10	15.987	18.307	20.463	23.209	25.188	29.588	31.420	
11	17.275	19.675	21.920	24.725	26.757	31.264	33.137	
12	18.549	21.026	23.337	26.217	28.300	32.909	34.821	
13	19.812	22.362	24.736	27.688	29.819	34.528	36.419	
14	21.064	23.685	26.119	29.141	31.319	36.123	38.109	
15	22.307	24.996	27.488	30.578	32.801	37.697	39.719	
16	23.542	26.296	28.845	32.000	34.267	39.252	41.308	
17	24.769	27.587	30.191	33.409	35.716	40.790	42.879	
18	25.989	28.869	31.526	34.805	37.156	42.312	44.434	
19	27.204	30.144	32.852	36.191	38.852	43.820	45.973	
20	28.412	31.410	34.170	37.566	39.967	45.315	47.498	
25	34.382	37.652	40.646	44.314	46.528	52.620	54.947	
30	40.256	43.773	46.979	50.892	53.672	59.703	62.162	
40	51.805	55.758	59.342	63.691	66.766	73.402	76.995	
50	63.167	67.505	71.420	76.154	79.490	86.661	89.561	
80	96.578	101.879	106.629	112.329	116.321	124.839	128.261	
∞	3.841	2.996	2.605	2.372	2.214	2.089	1.752	1.517

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ν_2	1	2	3	4	5	6	12	24	∞
ν_1	18.513	19.000	19.164	19.247	19.296	19.330	19.413	19.484	19.494
2	10.128	9.552	9.277	9.117	9.013	8.941	8.745	8.639	8.526
3	7.709	6.944	6.591	6.388	6.256	6.163	5.912	5.774	5.628
4	6.908	5.786	5.409	5.192	5.050	4.950	4.678	4.527	4.365
5	6.591	4.737	4.347	4.120	3.866	3.687	3.458	3.284	3.115
6	5.318	4.459	4.066	3.863	3.633	3.482	3.374	3.205	3.073
9	5.117	4.256	3.863	3.708	3.478	3.326	3.217	2.913	2.737
10	4.965	4.103	3.708	3.577	3.357	3.204	3.095	2.788	2.609
11	4.844	3.982	3.587	3.357	3.239	3.097	2.852	2.741	2.404
12	4.747	3.885	3.490	3.259	3.106	2.996	2.687	2.505	2.296
13	4.667	3.806	3.411	3.179	3.029	2.915	2.690	2.420	2.206
14	4.600	3.739	3.344	3.112	2.958	2.848	2.534	2.349	2.131
15	4.543	3.682	3.267	3.036	2.901	2.790	2.475	2.288	2.066
16	4.494	3.634	3.239	3.007	2.852	2.741	2.425	2.235	2.010
17	4.451	3.592	3.197	2.965	2.810	2.699	2.381	2.180	1.960
18	4.414	3.555	3.160	2.928	2.773	2.661	2.342	2.150	1.917
19	4.381	3.522	3.127	2.886	2.740	2.628	2.308	2.114	1.878
20	4.351	3.483	3.098	2.866	2.711	2.589	2.278	2.082	1.843
25	4.242	3.385	2.991	2.759	2.603	2.490	2.165	1.964	1.711
30	4.171	3.316	2.922	2.690	2.534	2.421	2.092	1.887	1.622
40	4.085	3.232	2.839	2.606	2.448	2.336	2.003	1.793	1.509
50	4.034	3.183	2.790	2.557	2.400	2.286	1.952	1.737	1.438
100	3.936	3.087	2.696	2.463	2.305	2.191	1.850	1.627	1.283
∞	3.841	2.996	2.605	2.372	2.214	2.089	1.752	1.517	1.002

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10 Percent Points of the F-Distribution

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TABLE A.4 Studentized Range Statistic

		K = Number of Means or Number of Steps Between Ordered Means										
		Error $(df \text{ within})$										
		1	2	3	4	5	6	7	8	9	10	11
ν_1	5	.05	3.64	4.60	5.22	5.67	6.03	6.33	6.56	6.80	6.99	7.17
	6	.05	5.70	6.98	8.42	8.91	9.32	9.67	9.97	10.24	10.48	
	7	.05	3.46	4.34	4.90	5.30	5.63	5.90	6.12	6.32	6.49	6.65
	8	.05	5.24	6.33	7.03	7.56	7.97	8.32	8.61	8.87	9.10	9.30
	9	.05	3.34	4.16	4.68	5.06	5.36	5.61	5.82	6.00	6.16	6.30
	10	.05	4.95	5.92	6.54	7.01	7.37	7.68	7.94	8.17	8.37	8.55
	11	.05	3.26	4.04	4.53	4.89	5.17	5.40	5.60	5.77	5.92	6.05
ν_2	5	.05	4.75	5.64	6.20	6.62	6.96	7.24	7.47	7.68	7.86	8.03
	6	.05	3.20	3.95	4.41	4.76	5.02	5.24	5.43	5.59	5.74	5.87
	7	.05	4.60	5.43	5.96	6.35	6.66	6.91	7.13	7.33	7.49	7.65
	8	.05	3.15	3.88	4.33	4.65	4.91	5.12	5.30	5.46	5.60	5.72
	9	.05	4.48	5.27	5.77	6.14	6.43	6.67	6.87	7.05	7.21	7.36
	10	.05	3.11	3.82	4.26	4.57	4.82	5.03	5.20	5.35	5.49	5.65
	11	.05	4.39	5.15	5.52	5.97	6.25	6.48	6.67	6.84	6.99	7.13
	12	.05	3.08	3.77	4.20	4.51	4.75	4.95	5.12	5.27	5.39	5.51
	13	.05	4.32	5.05	5.50	5.84	6.10	6.32	6.51	6.67	6.81	6.94
	14	.05	3.06	3.73	4.15	4.45	4.69	4.88	5.05	5.19	5.32	5.43
	15	.05	4.26	4.96	5.40	5.73	5.98	6.19	6.37	6.53	6.67	6.79
	16	.05	3.02	3.70	4.11	4.41	4.66	4.83	4.99	5.13	5.25	5.36
	17	.05	4.21	4.89	5.32	5.63	5.88	6.08	6.26	6.41	6.54	6.66
	18	.05	3.01	3.67	4.08	4.37	4.59	4.78	4.94	5.08	5.21	5.31
	19	.05	4.17	4.84	5.25	5.55	5.80	5.99	6.16	6.31	6.44	6.55
	20	.05	3.00	3.65	4.05	4.33	4.56	4.74	4.90	5.03	5.15	5.26
	21	.05	4.13	4.79	5.19	5.49	5.72	5.92	6.08	6.22	6.35	6.46
	22	.05	3.03	3.63	4.02	4.30	4.52	4.70	4.86	5.01	5.11	5.21
	23	.05	4.10	4.74	5.14	5.43	5.65	5.85	6.01	6.15	6.27	6.38
	24	.05	3.07	3.61	4.00	4.28	4.49	4.67	4.82	4.96	5.07	5.17
	25	.05	4.07	4.70	5.09	5.38	5.60	5.79	5.96	6.06	6.20	6.31
	26	.05	3.05	3.60	3.98	4.26	4.47	4.65	4.79	4.94	5.04	5.14
	27	.05	4.05	4.67	5.05	5.33	5.55	5.73	5.89	6.02	6.14	6.25
	28	.05	3.03	3.58	3.96	4.23	4.45	4.62	4.77	4.90	5.01	5.11
	29	.05	4.02	4.64	5.02	5.29	5.51	5.69	5.84	5.97	6.09	6.19
	30	.05	3.01	3.55	3.90	4.17	4.36	4.54	4.68	4.81	4.92	5.03
	31	.05	3.98	4.55	4.91	5.17	5.37	5.54	5.69	5.81	5.92	6.02
	32	.05	2.89	3.45	3.85	4.10	4.30	4.46	4.60	4.72	4.82	4.92
	33	.05	2.80	3.36	3.88	4.10	4.34	4.50	4.65	4.76	4.86	4.96
	34	.05	2.79	3.35	3.85	4.06	4.26	4.42	4.57	4.68	4.78	4.88
	35	.05	2.78	3.34	3.84	4.05	4.25	4.41	4.56	4.66	4.76	4.86
	36	.05	2.77	3.33	3.83	4.04	4.24	4.40	4.55	4.65	4.75	4.85
	37	.05	2.76	3.32	3.82	4.03	4.23	4.39	4.54	4.64	4.74	4.84
	38	.05	2.75	3.31	3.81	4.02	4.22	4.38	4.53	4.63	4.73	4.83
	39	.05	2.74	3.30	3.80	4.01	4.21	4.37	4.52	4.62	4.72	4.82
	40	.05	2.73	3.29	3.79	3.99	4.19	4.35	4.50	4.60	4.70	4.80
	41	.05	2.72	3.28	3.78	3.98	4.18	4.34	4.49	4.59	4.69	4.79
	42	.05	2.71	3.27	3.77	3.97	4.17	4.33	4.48	4.58	4.68	4.78
	43	.05	2.70	3.26	3.76	3.96	4.16	4.32	4.47	4.57	4.67	4.77
	44	.05	2.69	3.25	3.75	3.95	4.15	4.31	4.46	4.56	4.66	4.76
	45	.05	2.68	3.24	3.74	3.94	4.14	4.30	4.45	4.55	4.65	4.75
	46	.05	2.67	3.23	3.73	3.93	4.13	4.29	4.44	4.54	4.64	4.74
	47	.05	2.66	3.22	3.72	3.92	4.12	4.28	4.43	4.53	4.63	4.73
	48	.05	2.65	3.21	3.71	3.91	4.11	4.27	4.42	4.52	4.62	4.72
	49	.05	2.64	3.20	3.70	3.90	4.10	4.26	4.41	4.51	4.61	4.71
	50	.05	2.63	3.19	3.69	3.89	4.09	4.25	4.40	4.50	4.60	4.70
	51	.05	2.62	3.18	3.68	3.88	4.08	4.24	4.39	4.49	4.59	4.69
	52	.05	2.61	3.17	3.67	3.87	4.07	4.23	4.38	4.48	4.58	4.68
	53	.05	2.60	3.16	3.66	3.86	4.06	4.22	4.37	4.47	4.57	4.67
	54	.05	2.59	3.15	3.65	3.85	4.05	4.21	4.36	4.46	4.56	4.66
	55	.05	2.58	3.14	3.64	3.84	4.04	4.20	4.35	4.45	4.55	4.65
	56	.05	2.57	3.13	3.63	3.83	4.03	4.19	4.34	4.44	4.54	4.64
	57	.05	2.56	3.12	3.62	3.82	4.02	4.18	4.33	4.43	4.53	4.63
	58	.05	2.55	3.11	3.61	3.81	4.01	4.17	4.32	4.42	4.52	4.62
	59	.05	2.54	3.10	3.60	3.80	4.00	4.16	4.31	4.41	4.51	4.61
	60	.05	2.53	3.09	3.59	3.79	3.99	4.15	4.30	4.40	4.50	4.60
	61	.05	2.52	3.08	3.58	3.78	3.98	4.14	4.29	4.39	4.49	4.59
	62	.05	2.51	3.07	3.57	3.77	3.97	4.13	4.28	4.38	4.48	4.58
	63	.05	2.50	3.06	3.56	3.76	3.96	4.12	4.27	4.37	4.47	4.57
	64	.05	2.49	3.05	3.55	3.75	3.95	4.11	4.26	4.36	4.46	4.56
	65	.05	2.48	3.04	3.54	3.74	3.94	4.09	4.24	4.34	4.44	4.54
	66	.05	2.47	3.03	3.53	3.73	3.93	4.08	4.23	4.33	4.43	4.53
	67	.05	2.46	3.02	3.52	3.72	3.92	4.07	4.22	4.32	4.42	4.52
	68	.05	2.45	3.01	3.51	3.71	3.91	4.06	4.21	4.31	4.41	4.51
	69	.05	2.44	3.00	3.50	3.70	3.90	4.05	4.20	4.30	4.40	4.50
	70	.05	2.43	2.99	3.49	3.69	3.89	4.04	4.19	4.29	4.39	4.49
	71	.05	2.42	2.98	3.48	3.68	3.88	4.03	4.18	4.28	4.38	4.48
	72	.05	2.41	2.97	3.47	3.67	3.87	4.02	4.17	4.27	4.37	4.47
	73	.05	2.40	2.96	3.46	3.66	3.86	4.01	4.16	4.26	4.36	4.46
	74	.05	2.39	2.95	3.45	3.65	3.85	4.00	4.15	4.25	4.35	4.45
	75	.05	2.38	2.94	3.44	3.64	3.84	3.99	4.14	4.24	4.34	4.44
	76	.05	2.37	2.93	3.43	3.63	3.83	3.98	4.13	4.23	4.33	4.43
	77	.05	2.36	2.92	3.42	3.62	3.82	3.97	4.12	4.22	4.32	4.42
	78	.05	2.35	2.91	3.41	3.61	3.81	3.96	4.11	4.21	4.31	4.41
	79	.05	2.34	2.90	3.40	3.60	3.80	3.95	4.10	4.20	4.30	4.40
	80	.05	2.33	2.89	3.39	3.59	3.79	3.94	4.09	4.19	4.29	4.39
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