

UNIVERSITY OF SWAZILAND

MAIN EXAMINATION 2010

TITLE OF PAPER: INDIRECT TECHNIQUES FOR DEMOGRAPHIC ESTIMATION

COURSE NUMBER: DEM 303

TIME ALLOWED: 3 HOURS

INSTRUCTIONS: ANSWER QUESTION 1 AND 2 AND ANY TWO QUESTIONS FROM SECTION B. ALL QUESTIONS ARE WORTH 25 MARKS EACH.

REQUIREMENTS: CALCULATOR

THIS PAPER SHOULD NOT BE OPENED UNTIL PERMISSION HAS BEEN GIVEN BY THE INVIGILATOR

SECTION A: COMPULSORY (Answer all questions)

Question 1

- a) Describe the importance of indirect estimation in Demography. Elaborate your answer with examples.(4)
- b) Describe how you would select a model life table from the Coale and Demeny regional model life tables to use in specific demographic estimation. (4)
- c) Find the value of ${}_4q_1$ corresponding to level 13.8 in the female South model life table.(4)
- d) Find the value of ${}_3d_2$ corresponding to level 14.7 in the female North model life table.(4)
- e) What is the probability of surviving to age 4 in a population whose probability of surviving to age 5 is 0.785? Assume the male East model is applicable. (5)
- f) Give any two weaknesses/limitations of the Brass Growth Balance method for estimating the completeness of death registration.(4)

Question 2

- a) What are the assumptions of the Brass method for estimating childhood mortality using information from women on the proportion of children dead? (6)
- b) You are given the data below on average parity per woman and proportion of children dead classified by age group of women. Using Trussel's variant of the Brass method, calculate $q(2)$ and $q(3)$. (8)

Age group	i	Average parity	Proportion dead
15-19	1	0.170	0.0560
20-24	2	1.100	0.0817
25-29	3	2.360	0.0760

You may find the following information useful:

i	a(i)	b(i)	c(i)
1	1.0819	-3.0005	0.8689
2	1.2846	-0.6181	-0.3024
3	1.2223	0.0851	-0.4704

- c) Describe the problems associated with the reverse survival technique.(6)
- d) Give an interpretation of the parameters for the Coale-McNeil model for nuptiality. (5)

SECTION B (answer any 2 questions)

Question 3

- a) You are given the following life table values for a certain country. Estimate the values of α and β you would use to fit the Brass logit model to the data. (16)

Age	l_x
15	0.592
20	0.559
25	0.548
30	0.528
35	0.511
40	0.492
45	0.460
50	0.435

- b) What do the data suggest about the age pattern of mortality for this country? (3)
c) Use the values of the parameters obtained to estimate the values for l_{10} and l_{55} . (6)

Question 4

- a) What is the difference between relational models and parametric models? (5)
b) What is the difference between life table models and stable population models? (6)
c) What are the characteristics of a stable population? (6)
d) Describe the Sisterhood method for maternal mortality. Make sure to include the data requirements and computational procedures. (8)

Question 5

- a) What are the disadvantages of the widowhood method for estimating adult survivorship? (6)
b) Using the data on the proportion of ever married respondents classified by age given below, calculate the male probability of survival from age 20 to age 35 and from age 20 to 40. (10)

Age	$NW_f(n)$	$NW_f(n-5)$
30	0.8668	0.7408
35	0.9246	0.8668
40	0.9458	0.9246

You may find the following information useful:

n	a(n)	b(n)	c(n)	d(n)
30	-0.0284	-0.00465	0.00157	1.0822
35	-0.0159	-0.00638	0.00253	1.0831
40	-0.0041	-0.00784	0.00395	1.0596

Assume that $SMAM_m = 25.3$ years and $SMAM_f = 23.2$ years.

- c) What are the assumptions for the orphanhood method for estimating adult mortality? (6)
- d) One of the methods for estimating fertility is by using the increment of cohort parities between two surveys/censuses. Under what conditions is it appropriate to use this method? (3)

Question 6

- a) Give an interpretation of the parameters for the Brass Relational Gompertz model for fertility. (6)
- b) You are given the following age-specific marital fertility rates attained by a certain Christian religious group living in the USA for a certain period.

Age group	ASMFR
15-19	0.300
20-24	0.550
25-29	0.502
30-34	0.447
35-39	0.406
40-44	0.222
45-49	0.061

Use the Coale-Trussel model to estimate the parameters m and M you would use to fit the marital fertility schedule, using the least squares method. (15)

You may find the following information useful: $Y(i) = \ln [\Phi(i)/h(i)]$

- c) Give an interpretation of the parameters obtained above.(4)

TABLE XIV. Values of l_x by single years of age from 1 to 5 for regional model life tables ($k_0 = 100,000$) at mortality levels 1-24

LEVEL	M O D E L				W E S T				M A L E S						
	<i>Females</i>	l_1	l_2	l_3	l_4	<i>Females</i>	l_1	l_2	l_3	l_4	<i>Males</i>	l_1	l_2	l_3	l_4
1	63445	54958	51154	48696	46836	50650	50262	46851	44617	42957	66601	58514	52509	48663	47062
2	66601	58514	54891	52509	50776	51614	54105	50817	48663	47062	69444	61785	54456	48663	47062
3	69444	61785	58353	56135	54567	64826	57643	54957	52437	50905	72027	64811	61152	54957	52437
4	72027	64811	61578	59488	57907	67743	60918	57929	55972	54517	74389	67625	64213	57929	55972
5	74389	67625	64593	62834	61152	70411	63965	61142	59293	57919	76562	67251	64213	62424	61133
6	76562	70251	67423	65956	64213	72865	75135	69481	67004	65382	78571	72713	67107	67004	65382
7	78571	72713	70088	68391	67107	75135	72433	71992	69691	68185	80438	75028	71037	72433	68185
8	80438	75028	72604	71037	69852	79211	74547	72360	70846	67066	82178	74986	73547	72360	67066
9	82178	77211	74986	73547	72459	79211	74547	72360	70846	67066	83807	79276	75933	74547	67066
10	83807	79276	77246	75933	74940	81049	76601	74654	73378	72435	85336	81233	78206	72775	72435
11	85336	81233	79394	78206	77307	82775	78726	76953	75791	74928	86775	81441	79567	79144	74928
12	86775	83092	81441	80374	80374	84042	80745	82816	81428	80520	78092	82191	79567	78096	77316
13	88121	84865	83405	82062	81749	85983	84756	83560	82777	82194	89396	86413	84013	84756	82194
14	89396	86646	85413	84616	84013	87487	84756	83560	82777	82194	90606	88290	86357	87487	82194
15	90606	88290	86242	85659	86037	86804	85414	84235	83560	82777	91769	89864	88084	86632	86203
16	91769	89864	88987	88087	87954	90084	88086	88478	88976	88477	92884	91352	89772	89772	88477
17	92884	91352	90635	9053	89772	91322	89716	88976	88477	88098	93759	92192	91496	90244	89921
18	93759	92192	91496	90806	91496	92517	91266	91266	90662	90244	94089	93664	93134	92266	91672
19	94089	93664	93372	93372	93372	93666	93666	93666	92266	92266	95931	95347	94693	93545	93545
20	95931	95347	95059	94859	94859	94693	94693	94693	93791	93545	96884	96531	96231	95070	94937
21	96884	96531	96355	96231	96231	96127	95866	95660	95070	95070	97118	97507	97240	96391	96391
22	97118	97507	97400	97324	97260	96990	96648	96391	96391	96391	98470	98361	98230	97699	97552
23	98470	98361	98305	98264	98264	97838	97616	97616	97552	97552	99048	99024	99007	98548	98492
24	99048	99024	99024	99024	99024	98992	98652	98548	98548	98548	99555	99533	99533	99252	99240
25	99555	99533	99533	99533	99533	99527	99527	99527	99527	99527	99219	99219	99163	99252	99240
LEVEL	<i>Females</i>	l_1	l_2	l_3	l_4	<i>Females</i>	l_1	l_2	l_3	l_4	<i>Females</i>	l_1	l_2	l_3	l_4
LEVEL	<i>Females</i>	l_1	l_2	l_3	l_4	<i>Females</i>	l_1	l_2	l_3	l_4	<i>Females</i>	l_1	l_2	l_3	l_4
1	68005	59681	54557	50689	47753	51626	66052	54755	54755	53606	5109	46166	43381	46166	43381
2	70776	62905	58061	54403	51603	55232	68919	61570	61570	5770	51254	47449	47449	47449	47449
3	73263	65822	61290	57847	55232	58602	71515	64572	64572	60550	57212	54826	54826	54826	54826
4	75516	68564	64285	61055	58602	61763	73883	67354	67354	63382	60432	58187	58187	58187	58187
5	77570	71074	67074	64055	64055	64737	70657	69943	69943	66224	63461	61359	61359	61359	61359
6	79456	73407	69683	66871	66871	67543	78062	72362	72362	68895	66319	64360	64360	64360	64360
7	81196	75285	72130	69523	67543	70197	79920	74631	74631	71413	69023	67205	67205	67205	67205
8	82808	77625	74434	72025	70197	72712	81650	76764	76764	73193	69906	67586	67586	67586	67586
9	84308	79542	76608	74394	72712	76639	75101	83264	78777	78777	76018	74019	72477	72477	72477
10	85709	81349	78665	76639	75101	77373	84777	80679	80679	78187	76335	74927	74927	74927	74927
11	87022	83056	80615	78772	77373	80799	79535	89335	89335	89228	87730	77261	77261	77261	77261
12	88253	84670	82464	804302	82837	81724	87529	84247	84247	80218	78538	76538	76538	76538	76538
13	89398	86244	84302	82837	84770	83796	88709	85835	85835	84087	82789	81801	81801	81801	81801
14	90441	87759	86046	84770	84770	86609	85751	86609	85751	85852	83870	84726	84726	84726	84726
15	91453	89164	87717	86609	86609	88340	87595	90975	88909	87598	86608	85846	85846	85846	85846
16	92453	90521	89291	88340	88340	89971	89335	92054	90376	90376	89228	88399	87730	87730	87730
17	93372	91862	90773	89971	89971	91508	90978	93094	91759	91759	90899	89526	89526	89526	89526
18	94274	93012	92170	92959	92959	92531	94091	93061	92309	92309	91712	91237	91237	91237	91237
19	95136	94453	93487	92959	92959	94302	94091	95043	94286	94286	93706	92866	92866	92866	92866
20	95956	95230	94729	94330	94330	95043	94091	95401	95401	95401	95026	94691	94691	94691	94691
21	96736	96246	95904	95628	95628	95904	95401	96753	96826	96826	96290	95925	95925	95925	95925
22	97487	97221	97032	96879	96879	96753	96753	96753	96753	96753	97408	97134	97134	97134	97134
23	98122	97974	97867	97780	97780	97974	97780	97780	97780	97780	97580	97032	97032	97032	97032
24	98723	98618	98593	98593	98593	98593	98593	98593	98593	98593	98321	98022	98022	98022	98022
25	99219	99187	99163	99163	99163	99163	99163	99163	99163	99163	98944	98866	98866	98866	98866

TABLE XIV (Continued). Values of l_x by single years of age from 1 to 5 for regional model life tables ($t_0 = 100,000$) at mortality levels 1 to 24

LEVEL	t_0	M O D E L				E A S T				M O D E L				S O U T H						
		<i>Females</i>	l_1	l_2	l_3	l_4	l_1	l_2	l_3	l_4	<i>Males</i>	l_1	l_2	l_3	l_4	<i>Males</i>	l_1	l_2	l_3	l_4
1	57180	49795	46656	44596	43167	40453	42922	47063	42922	40206	38482	42922	44382	46644	48305	46644	45436	45436	45436	45436
2	60636	53494	50458	48466	47084	45211	50920	57211	50920	48303	48303	50399	52003	52003	52003	50399	49227	49227	49227	49227
3	63788	56935	54022	52111	50784	54290	60666	54530	60666	52003	52003	55963	55963	55963	55963	55963	52840	52840	52840	52840
4	66680	60150	57375	55554	54290	58815	63741	57920	63741	58814	58814	61115	61115	61115	61115	61115	56286	56286	56286	56286
5	69350	63168	60540	58815	57619	60786	66689	61913	66689	60540	60540	64135	64135	64135	64135	64135	59577	59577	59577	59577
6	71827	66009	63536	61913	60786	64860	69398	66689	69398	64860	64860	69962	69962	69962	69962	69962	65742	65742	65742	65742
7	74135	68692	66378	64860	63660	67670	71891	69453	71891	67670	67670	66620	66620	66620	66620	66620	68635	68635	68635	68635
8	76292	71232	69081	67670	66458	70350	74288	69453	74288	69081	69081	70555	70555	70555	70555	70555	69445	69445	69445	69445
9	78317	73643	71657	70350	69453	72920	76504	72474	76504	71524	71524	73249	73249	73249	73249	73249	71524	71524	71524	71524
10	80221	75936	74115	72920	71657	75464	77225	75699	77225	75464	75464	77144	77144	77144	77144	77144	74199	74199	74199	74199
11	82003	78166	76535	74115	72920	78828	77881	77881	77881	78828	78828	80519	80519	80519	80519	80519	74850	74850	74850	74850
12	83663	80270	78828	77881	77225	80191	79615	82373	79387	80191	80191	78145	78145	78145	78145	78145	77357	77357	77357	77357
13	85260	82285	81020	80191	79615	82397	81897	81897	81897	82397	82397	84161	84161	84161	84161	84161	81657	81657	81657	81657
14	86794	84213	83117	82397	81897	84207	85882	84504	85882	84207	84207	83626	83626	83626	83626	83626	82097	82097	82097	82097
15	88267	86059	85120	84207	83117	86059	86159	86159	86159	86059	86059	87536	87536	87536	87536	87536	83956	83956	83956	83956
16	89677	87823	87035	86059	85120	87823	88455	88455	88455	87823	87823	88123	88123	88123	88123	88123	86470	86470	86470	86470
17	91028	89531	88885	88455	87823	89531	90305	90305	90305	89531	89531	90643	90643	90643	90643	90643	88288	88288	88288	88288
18	92318	91160	90650	90305	89531	92328	92069	91877	92069	90305	90305	92095	92095	92095	92095	92095	90325	90325	90325	90325
19	93548	92706	92069	91877	91657	93275	93622	93622	93622	92706	92706	93480	93480	93480	93480	93480	92249	92249	92249	92249
20	94721	94176	93927	93622	93275	94537	95171	95171	95171	94721	94721	94462	94462	94462	94462	94462	94018	94018	94018	94018
21	95904	95546	95380	95171	94537	95262	95171	95171	95171	95904	95904	96111	96111	96111	96111	96111	95574	95574	95574	95574
22	96939	96718	96614	96539	95546	96614	96539	96539	96539	96939	96939	97245	97245	97245	97245	97245	96935	96935	96935	96935
23	97861	97739	97681	97638	96614	97861	97638	97638	97638	97861	97861	98116	98116	98116	98116	98116	98088	98088	98088	98088
24	98640	98583	98555	98535	97681	98640	98535	98535	98535	98640	98640	98989	98989	98989	98989	98989	98936	98936	98936	98936
25	99245	99223	99212	99204	98640	99245	99204	99204	99204	99223	99223	99229	99229	99229	99229	99229	97357	97357	97357	97357
1	69279	55503	49161	45812	43909	47727	52655	49512	47727	52655	52655	57056	57056	57056	57056	57056	48164	48164	48164	48164
2	71522	58606	52111	50784	48466	51304	55913	52914	50784	52111	52111	59951	59951	59951	59951	59951	48694	48694	48694	48694
3	73567	61479	56225	54290	51304	58964	61852	59287	58964	56225	56225	62645	62645	62645	62645	62645	50567	50567	50567	50567
4	75420	64651	61832	59287	57842	6218	64537	60843	6218	64651	64651	65163	65163	65163	65163	65163	52667	52667	52667	52667
5	77119	66651	64651	6218	60843	66997	64537	64537	64537	66651	66651	67526	67526	67526	67526	67526	53846	53846	53846	53846
6	78685	68685	66651	64651	6218	67094	64923	63689	64923	66651	66651	67500	67500	67500	67500	67500	55267	55267	55267	55267
7	80136	71206	69518	67525	66394	69518	67525	67525	67525	71206	71206	71850	71850	71850	71850	71850	66351	66351	66351	66351
8	81487	73291	69518	67525	66394	71820	70001	68968	70001	69518	69518	80975	80975	80975	80975	80975	68781	68781	68781	68781
9	82748	75265	73291	71820	70001	74028	71445	73636	71445	73291	73291	72629	72629	72629	72629	72629	70990	70990	70990	70990
10	83916	77145	74028	71445	73636	76106	76795	76034	76795	77145	77145	77434	77434	77434	77434	77434	72446	72446	72446	72446
11	84937	78890	80569	78099	76034	80569	80011	78863	80011	78890	78890	84419	84419	84419	84419	84419	74702	74702	74702	74702
12	85933	81342	82184	80845	80011	82184	83338	81845	83338	82184	82184	85474	85474	85474	85474	85474	76867	76867	76867	76867
13	86903	82016	90774	90064	90774	92016	91496	91496	91496	92016	92016	86501	86501	86501	86501	86501	77504	77504	77504	77504
14	87848	88764	94089	93226	92475	92475	92475	92475	92475	94089	94089	93372	93372	93372	93372	93372	78943	78943	78943	78943
15	88764	85232	83606	82260	82260	84573	85297	84573	84573	88764	88764	87498	87498	87498	87498	87498	80935	80935	80935	80935
16	89651	86610	85232	83606	82260	84573	84573	84573	84573	89651	89651	88463	88463	88463	88463	88463	82446	82446	82446	82446
17	90509	88668	86924	88523	88038	87751	86967	89440	87751	90509	90509	90303	90303	90303	90303	90303	86457	86457	86457	86457
18	91342	92266	90774	90064	90774	92016	91496	91496	91496	92016	92016	91361	91361	91361	91361	91361	88727	88727	88727	88727

TABLE 3. STANDARD PATTERN OF NATURAL FERTILITY AND OF DEVIATIONS FROM NATURAL FERTILITY, BY AGE GROUP, FOR THE COALE AND TRUSSELL FERTILITY MODEL.

Age group (i)	Index i	Natural fertility $\bar{N}(i)$	Deviation pattern	
			(2)	from natural fertility $\bar{N}(i)$ (4)
15-19	1	0.411	0.000
20-24	2	0.460	0.000
25-29	3	0.431	-0.279
30-34	4	0.395	-0.667
35-39	5	0.322	-1.042
40-44	6	0.167	-1.414
45-49	7	0.024	-1.671

ANNEX II

General and African Standard Life Table l_x 's and Logits

<u>General standard</u>			<u>African standard</u>		
x	l_x	$Y_x(x)$	x	l_x	$Y_x(x)$
0	1.0000		0	1.0000	
1	0.8499	-0.8670	1	0.8802	-0.9972
2	0.8070	-0.7153	2	0.8335	-0.8053
3	0.7876	-0.6553	3	0.8101	-0.7253
4	0.7762	-0.6218	4	0.7964	-0.6820
5	0.7691	-0.6016	5	0.7863	-0.6514
10	0.7502	-0.5498	10	0.7502	-0.5498
15	0.7362	-0.5131	15	0.7362	-0.5131
20	0.7130	-0.4551	20	0.7130	-0.4551
25	0.6826	-0.3829	25	0.6326	-0.3829
30	0.6525	-0.3150	30	0.6525	-0.3150
35	0.6223	-0.2496	35	0.6223	-0.2496
40	0.5898	-0.1817	40	0.5898	-0.1817
45	0.5535	-0.1073	45	0.5535	-0.1073
50	0.5106	-0.0212	50	0.5106	-0.0212
55	0.4585	0.0832	55	0.4585	0.0832
60	0.3965	0.2100	60	0.3965	0.2100
65	0.3210	0.3746	65	0.3210	0.3746
70	-0.2380	0.5818	70	-0.2380	0.5818
75	0.1516	0.8611	75	0.1516	0.8611
80	0.0768	1.2433	80	0.0768	1.2433
85	0.0276	1.7810	85	0.0276	1.7810
90	0.0059	2.5634	90	0.0059	2.5634
95	0.0006	3.7090	95	0.0006	3.7090
100	0.0000		100	0.0000	

Source: Carrier and Hobcraft (1973) (These are the smoothed and extended versions of the original standard)