

UNIVERSITY OF SWAZILAND

MAIN EXAMINATION 2008

**TITLE OF PAPER: INDIRECT TECHNIQUES FOR DEMOGRAPHIC
ESTIMATION**

CORSE NUMBER: DEM 303

TIME ALLOWED: 3 HOURS

**INSTRUCTIONS: ANSWER QUESTION 1 AND ANY THREE QUESTIONS.
ALL QUESTIONS ARE WORTH 20 MARKS EACH.**

REQUIREMENTS: CALCULATOR

**THIS PAPER SHOULD NOT BE OPENED UNTIL PERMISSION HAS BEEN
GIVEN BY THE INVIGILATOR**

SECTION A: Compulsory

Question 1

Describe any two of the following indirect estimation methods. Make sure to include the data requirements and computational procedures of each method. (20)

- a) Sisterhood method
- b) Orphanhood method
- c) Brass P/F Ratio method

SECTION B (answer any 2 questions)

Question 2

- a) What are the uses of the Brass logit system? (6)
- b) Fit the Brass logit model on the following table:

Age (x)	lx
15	96457
20	95800
25	94912
30	94042
35	93044
40	91645
45	89537
50	86259

- c) What are the meanings of the Brass parameters obtained above? (4)

Question 3

- a) One method of estimating fertility is by using the increment of cohort parities between two surveys/censuses. Under what conditions is it appropriate to use this method? (5)
- b) The data below shows the average parities of women at two surveys 5 years apart $P(i, 1)$ and $P(i, 2)$. Using the data calculate, the inter-survey age-specific fertility rates $f(1, s)$, $f(2, s)$ and $f(3, s)$. (15)

Age	i	$P(i, 1)$	$P(i, 2)$
15-19	1	0.131	0.127
20-24	2	0.994	0.884
25-29	3	2.409	2.126
30-34	4	3.819	3.481
35-39	5	5.082	4.660
40-44	6	5.921	5.677

You may find the following formula useful:

$$\Phi(i,s) = 0.9283 P(i,s) + 0.4547 P(i+1,s) - 0.0585 P(i+2,s) - 0.3245 \Phi(i-1,s);$$

Where $P(i, s) = P(i-1, s) + P(i, 2) - P(i-1, 1)$ or $P(i,s) = \sum \Delta P(j)$

Question 4

- a) State the assumptions of the widowhood method. (6)
- b) What are the advantages of the widowhood method over the orphanhood method? (6)
- c) Using the data on the proportion of ever married respondents classified by age given below, calculate the male probability of survival from age 20 to age 35 and from age 20 to 40. (8)

Age	$NW_f(n)$	$NW_f(n-5)$
30	0.9514	0.9729
35	0.9170	0.9514
40	0.8735	0.9170

You may find the following information useful:

n	a (n)	b (n)	c (n)	d (n)
30	-0.0284	-0.00465	0.00157	1.0822
35	-0.0159	-0.00638	0.00253	1.0831
40	-0.0041	-0.00784	0.00395	1.0596

Assume that SMAM (m) = 25.3 years and SMAM (f) = 23.2 years.

Question 5

- Find the value of $4q_1$ corresponding to level 13.8 in the female South model life table. (4)
- Find the value of ${}_3d_2$ corresponding to level 14.7 in the female North model life table. (6)
- What is the probability of surviving to age 4 in a population whose probability of surviving to age 5 is 0.785? Assume the male North model is applicable. (6)
- Using the West model, compute the percentage change in the under 5 female mortality when the level changes from 9 to 10. (4)

Question 6

- What is meant by demographic models? Describe any three uses of demographic models. (8)
- Point out two similarities and two differences between the Coale-Demeny life tables and the United Nations model life tables for developing countries. (4)
- Specify the family of life tables that would best represent the mortality pattern in the following populations:
 - A population with high malnutrition among infants and children. (2)
 - A population with high incidence of neonatal tetanus. (2)
 - A population with high mortality during infancy and childhood years and young adults. (2)
 - A population with high male death rate at older ages in relation to their death rates at younger ages. (2)

ANNEX II

General and African Standard Life Table l_x 's and Logits

General standard			African standard		
x	l_x	$Y_x(x)$	x	l_x	$Y_x(x)$
0	1.0000		0	1.0000	
1	0.8499	-0.8670	1	0.8802	-0.9972
2	0.8070	-0.7153	2	0.8335	-0.8053
3	0.7876	-0.6553	3	0.8101	-0.7253
4	0.7762	-0.6218	4	0.7964	-0.6820
5	0.7691	-0.6016	5	0.7863	-0.6514
	0.7502	-0.5498	10	0.7502	-0.5498
	0.7362	-0.5131	15	0.7362	-0.5131
20	0.7130	-0.4551	20	0.7130	-0.4551
25	0.6826	-0.3829	25	0.6326	-0.3829
30	0.6525	-0.3150	30	0.6525	-0.3150
35	0.6223	-0.2496	35	0.6223	-0.2496
40	0.5898	-0.1817	40	0.5898	-0.1817
45	0.5535	-0.1073	45	0.5535	-0.1073
50	0.5106	-0.0212	50	0.5106	-0.0212
55	0.4585	0.0832	55	0.4585	0.0832
60	0.3965	0.2100	60	0.3965	0.2100
65	0.3210	0.3746	65	0.3210	0.3746
70	0.2380	0.5818	70	0.2380	0.5818
75	0.1516	0.8611	75	0.1516	0.8611
80	0.0768	1.2433	80	0.0768	1.2433
85	0.0276	1.7810	85	0.0276	1.7810
90	0.0059	2.5634	90	0.0059	2.5634
95	0.0006	3.7090	95	0.0006	3.7090
100	0.0000		100	0.0000	

Source: Carrier and Hobcraft (1973) (These are the smoothed and extended versions of the original standard)

Table XIV. Values of l_x by single years of age from 1 to 5 for regional model life tables ($l_0 = 100,000$) at mortality levels 1-24

W E S T										N O R T H									
M O D E L					F o r m u l a					M o d e l					M o d e l				
L E V E L	l_1	l_2	l_3	l_4	l_1	l_2	l_3	l_4	l_1	l_2	l_3	l_4	l_1	l_2	l_3	l_4	l_1	l_2	
1	63445	51958	51154	48696	46836	50050	50262	46617	46851	50262	50650	50262	46617	46851	46617	46617	42957	47062	
2	66601	52549	50714	52549	56135	56135	56135	56135	54063	54063	54063	54063	54063	54063	54063	54063	47062	50906	
3	69614	61765	58353	58353	54498	54498	54498	54498	54497	54497	54497	54497	54497	54497	54497	54497	54497	54497	
4	72027	64811	61578	61578	57907	57907	57907	57907	67743	67743	67743	67743	67743	67743	67743	67743	55917	55917	
5	74389	67625	64593	64593	62634	62634	62634	62634	61132	61132	61132	61132	61132	61132	61132	61132	55923	55923	
6	76662	70251	67423	67423	65596	65596	65596	65596	72665	72665	72665	72665	66812	66812	66812	66812	64160	64160	
7	78571	72713	70088	70088	68391	68391	68391	68391	67107	67107	67107	67107	67243	67243	67243	67243	67004	67004	
8	80138	75328	72604	72604	71037	71037	71037	71037	70845	70845	70845	70845	71992	71992	71992	71992	68185	68185	
9	82178	77211	74986	74986	73547	73547	73547	73547	72459	72459	72459	72459	72029	72029	72029	72029	69813	69813	
10	83807	79776	77246	77246	74940	74940	74940	74940	76601	76601	76601	76601	74654	74654	74654	74654	72440	72440	
11	85316	81233	79394	79394	76206	76206	76206	76206	77307	77307	77307	77307	82775	82775	82775	82775	76953	76953	
12	86775	83092	81441	81441	80374	80374	80374	80374	79567	79567	79567	79567	88045	88045	88045	88045	78096	78096	
13	88121	84665	82462	82462	81749	81749	81749	81749	82903	82903	82903	82903	82166	82166	82166	82166	80520	80520	
14	89396	86446	85413	85413	84616	84616	84616	84616	84487	84487	84487	84487	84756	84756	84756	84756	82777	82777	
15	90506	88290	87242	87242	86559	86559	86559	86559	86047	86047	86047	86047	86446	86446	86446	86446	84235	84235	
16	91789	89664	88947	88947	88407	88407	88407	88407	87954	87954	87954	87954	88084	88084	88084	88084	8632	8632	
17	92884	91352	90635	90635	90153	90153	90153	90153	89712	89712	89712	89712	91322	91322	91322	91322	88477	88477	
18	93969	92759	92192	92192	91806	91806	91806	91806	91196	91196	91196	91196	90662	90662	90662	90662	90244	90244	
19	94665	94069	93664	93664	93372	93372	93372	93372	93134	93134	93134	93134	93666	93666	93666	93666	91913	91913	
20	95291	95547	95059	95059	94859	94859	94859	94859	94693	94693	94693	94693	94129	94129	94129	94129	93333	93333	
21	96884	96331	96335	96335	96127	96127	96127	96127	96127	96127	96127	96127	95666	95666	95666	95666	95070	95070	
22	97718	97107	97400	97400	97324	97324	97324	97324	97260	97260	97260	97260	96901	96901	96901	96901	96391	96391	
23	98470	98161	98305	98305	98264	98264	98264	98264	98220	98220	98220	98220	97838	97838	97838	97838	97499	97499	
24	99095	99046	99024	99024	99007	99007	99007	99007	99527	99527	99527	99527	98928	98928	98928	98928	99240	99240	
25	99555	99340	99340	99340	99333	99333	99333	99333	99333	99333	99333	99333	99333	99333	99333	99333	99333	99333	
L E V E L	l_1	l_2	l_3	l_4	l_1	l_2	l_3	l_4	l_1	l_2	l_3	l_4	l_1	l_2	l_3	l_4	l_1	l_2	
1	68005	59681	54557	50689	47753	62858	54755	54755	58063	58063	58063	58063	58313	58313	58313	58313	49228	49228	
2	70776	62905	57326	58061	5403	51626	51626	51626	68919	68919	68919	68919	61570	61570	61570	61570	50109	50109	
3	75516	73263	68564	61280	57487	55232	57151	57151	64572	64572	64572	64572	60550	60550	60550	60550	51254	51254	
4	77570	77570	74055	64285	61055	58602	67344	67344	71763	71763	71763	71763	63182	63182	63182	63182	50826	50826	
5	79456	73407	69681	67074	64055	61763	64737	64737	76057	76057	76057	76057	66943	66943	66943	66943	50167	50167	
6	71196	75585	72130	69233	66811	66811	67543	67543	76124	76124	76124	76124	76895	76895	76895	76895	61359	61359	
7	82808	76608	74434	72025	70197	70197	70197	70197	71920	71920	71920	71920	74631	74631	74631	74631	61602	61602	
8	94308	79542	76608	74434	72025	70197	70197	70197	61650	61650	61650	61650	76764	76764	76764	76764	75906	75906	
9	105709	81349	78665	76665	76639	75101	76777	76777	67373	67373	67373	67373	80679	80679	80679	80679	72477	72477	
10	87022	83056	80615	78772	78772	78772	78772	78772	65196	65196	65196	65196	82479	82479	82479	82479	76335	76335	
11	88253	84670	82464	80799	80799	79535	79535	79535	66196	66196	66196	66196	84247	84247	84247	84247	77261	77261	
12	89398	66244	84302	82887	82887	82887	82887	82887	67529	67529	67529	67529	84220	84220	84220	84220	80667	80667	
13	90441	67729	66046	84770	83196	83196	83196	83196	68709	68709	68709	68709	85835	85835	85835	85835	82769	82769	
14	91453	89164	87717	86609	85751	85751	85751	85751	86985	86985	86985	86985	87367	87367	87367	87367	88070	88070	
15	92431	90521	88291	88310	88310	88310	88310	88310	89717	89717	89717	89717	89755	89755	89755	89755	86546	86546	
16	93372	91802	90773	90773	90773	90773	90773	90773	91707	91707	91707	91707	92054	92054	92054	92054	88339	88339	
17	94274	93012	92170	92170	92170	92170	92170	92170	93487	93487	93487	93487	91759	91759	91759	91759	87236	87236	
18	95136	94153	93487	92959	92959	92959	92959	92959	94153	94153	94153	94153	94091	94091	94091	94091	92337	92337	
19	95956	95230	94729	94729	94729	94729	94729	94729	95044	95044	95044	95044	94286	94286	94286	94286	92666	92666	
20	96736	96246	95904	95904	95904	95904	95904	95904	95628	95628	95628	95628	95437	95437	95437	95437	94420	94420	
21	97467	97221	97032	96869	96869	96869	96869	96869	96753	96753	96753	96753	96826	96826	96826	96826	95925	95925	
22	98122	97974	97867	97867	97780	97780	97780	97780	96321	96321	96321	96321	97550	97550	97550	97550	92332	92332	
23	98123	98648	98548	98548	98510	98510	98510	98510	98630	98630	98630	98630	98108	98108	98108	98108	90222	90222	
24	99144	99167	99167	99167	99167	99167	99167	99167	99167	99167	99167	99167	98834	98834	98834	98834	98834	98834	
25	99219	99163	99163	99163	99163	99163	99163	99163	99163	99163	99163	99163	98944	98944	98944	98944	98834	98834	

TABLE XIV (Continued). Values of i_t by single years of age from 1 to 5 for regional model life tables ($i_0 = 100,000$) at mortality levels 1 to 24

LEVEL	i_1	MODEL					M_{0t+1}	i_t	i_t
		i_2	i_3	i_4	i_5	EAST			
1	57180	49795	46656	44986	43167	49453	42922	40206	38482
2	60636	53494	50458	48486	47084	53511	47063	44862	42680
3	63788	56935	52111	50784	52111	57211	50920	48305	46644
4	66680	60150	57375	55395	54290	60606	54330	52003	50399
5	69350	63168	60540	58815	57619	63741	57920	55500	53963
6	71827	66092	68925	66378	64660	66649	61115	58814	57351
7	74135	68922	71232	69081	67670	69690	64135	60584	59577
8	76292	71657	7053	69446	74266	66997	61891	61963	61725
9	78317	73936	74115	72920	72090	76504	69715	67822	66620
10	80211	82003	78166	76535	74722	78599	72932	70555	69445
11	81663	80270	78828	77681	77225	80519	7744	72249	71520
12	8285	81020	80191	79615	82373	7987	7541	74850	74199
13	83260	84285	82197	81897	81461	80461	80461	79770	79266
14	86794	84213	83117	82197	80807	85882	83626	82092	81657
15	86267	86059	85120	84546	84546	86519	85624	84929	83956
16	89677	87823	87035	86518	86518	87123	87544	86487	86166
17	90228	89511	88805	88445	88445	90055	90643	88879	88288
18	92318	91160	90650	90305	90305	91879	9120	90529	90325
19	93546	92707	92328	92059	91875	92095	92897	92220	92429
20	94721	94176	93927	93733	93622	93480	94462	94226	94018
21	95904	9546	95610	95292	95292	95171	95868	95741	95648
22	96839	96718	96614	96539	96539	96461	97110	97035	96935
23	97861	97739	97681	97638	97638	97245	98116	98088	98065
24	98640	98503	98555	98555	98555	98219	98989	98936	98926
25	99245	99223	99212	99204	99204	99198	98963		
LEVEL	i_1	MODEL					M_{0t+1}	i_t	i_t
		i_2	i_3	i_4	i_5	SOUTH			
1	69279	5503	49161	45812	43909	66423	53927	49164	43166
2	71532	5806	52655	49512	47777	66855	51056	51612	48894
3	73567	6179	55913	52974	51304	71056	59951	54829	52023
4	75420	64152	58964	56225	54668	73058	62645	57842	53446
5	77119	66651	61832	59287	57882	74894	65163	60675	58269
6	78665	68997	64537	62181	60883	76586	63347	61107	59270
7	80136	71266	61094	64923	63669	76154	69750	65874	63396
8	81487	73291	69516	67525	66384	79613	71850	68270	66331
9	82748	75265	71820	70001	68968	80975	73838	70546	68781
10	83916	77445	74028	72382	71492	82229	75650	72616	70992
11	84937	78690	76106	74636	73801	83337	77434	74711	73222
12	85933	80569	78099	76795	76054	84419	79153	76724	74742
13	86903	82184	80011	78863	78211	85474	80809	78657	77004
14	87646	83138	81845	80846	80278	85501	82405	80515	79502
15	88764	85212	81606	82246	82246	84160	87498	84300	80315
16	89651	86610	82297	84571	84571	86463	85419	84641	82446
17	90509	88068	86336	86334	85986	86397	86663	85603	84682
18	91342	89424	88823	88751	88076	87751	87270	86719	86437
19	92266	90774	90064	89676	89440	91361	89859	89132	88127
20	93180	9204	91496	91193	91004	92169	92657	91237	90150
21	94089	9326	92449	92449	92475	93737	92551	92123	91612
22	94988	94405	94116	93952	93846	94167	93106	93106	93190
23	95866	95484	95392	95181	95108	95343	94765	94637	94525
24	96716	96483	96165	96249	96249	96287	96064	95914	95799
25	97514	97366	97282	97282	97282	97282	97282	96984	96337