



UNIVERSITY OF ESWATINI

SECOND SEMESTER MAIN EXAMINATION PAPER, NOVEMBER 2021

FACULTY OF SOCIAL SCIENCES

DEPARTMENT OF ECONOMICS

COURSE CODE: ECO420

TITLE OF PAPER: ECONOMETRIC METHODS II

TIME ALLOWED: 2 HOURS

Instructions

1. This paper consists of two (2) sections, A and B
2. Section A, is compulsory and carries 40 marks
3. Section B, contains three (3) questions
4. Answer any other two (2) questions in Section B

Special Requirements

Scientific calculator

Additional Material (s)

None

DO NOT turn examination paper over until instructed to do so.

SECTION A

[40]

Question 1 Compulsory

- a) Table 1 presents data on management fees that a leading mutual fund firm in the US pays to its investment advisors to manage its assets. The fees depend on the net asset value of the fund. The higher the net asset value of the fund the lower the advisory fees. The distribution of management fees can be assumed to follow an exponential growth function $Y_i = \beta_1 e^{\beta_2 X_i + u_i}$. Use direct optimization to determine the estimates that minimize the sum of squares of the error. [15]

Table 1

| | Fee % | Net Asset Value in Billions |
|----|--------|-----------------------------|
| 1 | 0.52 | 0.5 |
| 2 | 0.508 | 5 |
| 3 | 0.484 | 10 |
| 4 | 0.46 | 15 |
| 5 | 0.4398 | 20 |
| 6 | 0.4238 | 25 |
| 7 | 0.4115 | 30 |
| 8 | 0.402 | 35 |
| 9 | 0.3944 | 40 |
| 10 | 0.388 | 45 |
| 11 | 0.3825 | 55 |
| 12 | 0.3738 | 60 |

- b) When $J=2$, we form $J-1=1$ non redundant logits, when $J>2$, we can form $J-1$ non redundant logits. Prove this statement. [7]
- c) Suppose we have count data which can be modelled using the Poisson Distribution with parameters (λ) . Prove that $\lambda = E[X] = E[X - E[X]]^2$ [8]
- d) Suppose we want to estimate the association of Aspirin Use on Myocardial Infarction. Calculate the generalized odds ratio, random row or column odds ratio and the reference category odds ratio and interpret the result. [6]

Table 2

| | Fatal Attack | Myocardial Infarction Nonfatal Attack | No Attack |
|---------|--------------|---------------------------------------|-----------|
| Placebo | 18 | 171 | 10845 |
| Aspirin | 5 | 99 | 10933 |

- e) What is panel data? [2]
- f) What are the drawbacks of relying on the coefficient of determination? [2]

SECTION B

ANSWER ANY TWO QUESTIONS

[30]

Question 2

- a) Suppose you are a research consultant hired by the Deputy Prime Minister's Office to conduct a study on employment sector preferences by sex. The aim is to find out which characteristics determine employment in the public sector, private sector and the informal sector. The following output is obtained from running the data.

Table 2: Model Fitting Information

| | Women | Men |
|-------------------------|---------|--------|
| Number of observations | 1567 | 2043 |
| LR chi2(38) | 1077.42 | 828.1 |
| Prob > chi ² | 0.0000 | 0.0000 |
| Pseudo R ² | 0.3342 | 0.241 |

Table 3: Test for Independence of Irrelevant Alternatives (Females)

| Omitted | lnL(full) | lnL(omit) | chi2 | df | P>chi2 | evidence |
|-------------------------|-----------|-----------|--------|----|--------|----------|
| Formal Public Sector | -301.809 | -296.145 | 11.328 | 20 | 0.937 | for Ho |
| Informal Private Sector | -217.252 | -207.92 | 18.664 | 20 | 0.544 | for Ho |
| Formal Private Sector | -109.108 | -97.256 | 23.704 | 20 | 0.256 | for Ho |

Table 4: Test for Independence of Irrelevant Alternatives (Males)

| Omitted | lnL(full) | lnL(omit) | chi2 | df | P>chi2 | evidence |
|-------------------------|-----------|-----------|--------|----|--------|----------|
| Formal Public Sector | -276.608 | -271.078 | 11.059 | 20 | 0.945 | for Ho |
| Informal Private Sector | -339.212 | -329.412 | 19.601 | 20 | 0.483 | for Ho |
| Formal Private Sector | -134.405 | -125.092 | 18.626 | 20 | 0.546 | for Ho |

Table 5: Multinomial Logit Model Results (Female)

| | Formal Public Sector | | Informal Private Sector | |
|-----------------------|----------------------|------------|-------------------------|------------|
| | Coefficient | Odds Ratio | Coefficient | Odds Ratio |
| age | 0.0521*** | 1.0534 | 0.0463*** | 1.0474 |
| Administrative Region | | | | |
| Manzini | -0.0436 | 0.9573 | 0.3787** | 1.4604 |
| Shiselweni | 0.6267** | 1.8714 | 0.2727 | 1.3135 |
| Lubombo | -0.3187 | 0.7271 | 0.2042 | 1.2265 |
| Geographic Location | | | | |
| Urban | -0.9692*** | 0.3794 | -0.8385*** | 0.4324 |
| Marital Status | | | | |

| | | | | |
|---|------------|---------|------------|----------|
| <i>Married</i> | 0.8247*** | 2.2812 | 0.5103*** | 1.6658 |
| <i>Widowed</i> | -0.5322 | 0.5873 | 0.4636* | 1.5898 |
| <i>Divorced</i> | 0.3264 | 1.3860 | 0.4403 | 1.5532 |
| Household Position | | | | |
| <i>Head</i> | 0.4939** | 1.6388 | 0.1172 | 1.1244 |
| Educational Attainment | | | | |
| <i>Elementary</i> | 0.7453 | 2.1071 | 0.1633 | 1.1774 |
| <i>High school</i> | 2.1502*** | 8.5864 | -0.7444*** | 0.4750 |
| <i>Vocational and College</i> | 3.4309*** | 30.9037 | -1.7894*** | 0.1671 |
| <i>University</i> | 3.3563*** | 28.6834 | -34.3019 | 1.27E-15 |
| Industrial Classification | | | | |
| <i>Agriculture and mining</i> | -2.7905*** | 0.0614 | -0.5437 | 0.5806 |
| <i>Manufacturing</i> | -2.8310*** | 0.0590 | -0.2932 | 0.7459 |
| <i>Electricity and water</i> | -0.6854 | 0.5039 | -33.1531 | 4.00E-15 |
| <i>Construction</i> | 0.6803 | 1.9744 | 1.2305 | 3.4230 |
| <i>Wholesale, retail trade and hospitality industry</i> | -3.5288*** | 0.0293 | 1.3061*** | 3.6920 |
| <i>Transportation and storage</i> | -0.2749 | 0.7596 | 0.2183 | 1.2440 |
| constant | -4.2101*** | | -2.3160*** | |

*Significant at 10%, **Significant at 5%, *** Significant at 1%

Table 6: Multinomial Logit Results Male

| | Formal Public Sector | | Informal Private Sector | |
|------------------------|----------------------|------------|-------------------------|------------|
| | Coefficient | Odds Ratio | Coefficient | Odds Ratio |
| age | 0.0215*** | 1.0217 | 0.0157** | 1.0158 |
| Administrative Region | | | | |
| <i>Manzini</i> | 0.0356 | 1.0363 | 0.2223 | 1.2489 |
| <i>Shiselweni</i> | 0.7093*** | 2.0325 | 0.2856 | 1.3306 |
| <i>Lubombo</i> | -0.3155 | 0.7294 | -0.3059 | 0.7365 |
| Geographic Location | | | | |
| <i>Urban</i> | -0.7578*** | 0.4687 | -0.6159*** | 0.5402 |
| Marital Status | | | | |
| <i>Married</i> | 0.3748** | 1.4548 | -0.4305** | 0.6502 |
| <i>Widowed</i> | 0.1237 | 1.1317 | -0.4054 | 0.6667 |
| <i>Divorced</i> | 0.2629 | 1.3007 | -0.1384 | 0.8708 |
| Household Position | | | | |
| <i>Head</i> | 0.0576 | 1.0593 | 0.1784 | 1.1953 |
| Educational Attainment | | | | |
| <i>Elementary</i> | -0.1973 | 0.8210 | -0.3380 | 0.7132 |
| <i>High School</i> | 0.7143*** | 2.0427 | -0.4510* | 0.6370 |

| | | | | |
|---|------------|--------|------------|--------|
| <i>Vocational and College Education</i> | 1.6860*** | 5.3981 | -0.8240* | 0.4387 |
| <i>University</i> | 1.7338*** | 5.6619 | -1.8534** | 0.1567 |
| Industrial Classification | | | | |
| <i>Agriculture and mining</i> | -1.9861*** | 0.1372 | -1.6642*** | 0.1893 |
| <i>Manufacturing</i> | -3.1148*** | 0.0444 | -1.3683*** | 0.2545 |
| <i>Electricity and water</i> | 0.4582 | 1.5812 | 0.3352 | 1.3983 |
| <i>Construction</i> | -2.1335*** | 0.1184 | 0.4884** | 1.6298 |
| <i>Wholesale, retail trade and hospitality industry</i> | -3.4851*** | 0.0307 | 0.1859 | 1.2043 |
| <i>Transportation and storage</i> | -1.7685*** | 0.1706 | -0.8747*** | 0.4170 |
| constant | -1.4302*** | | -1.1551*** | |

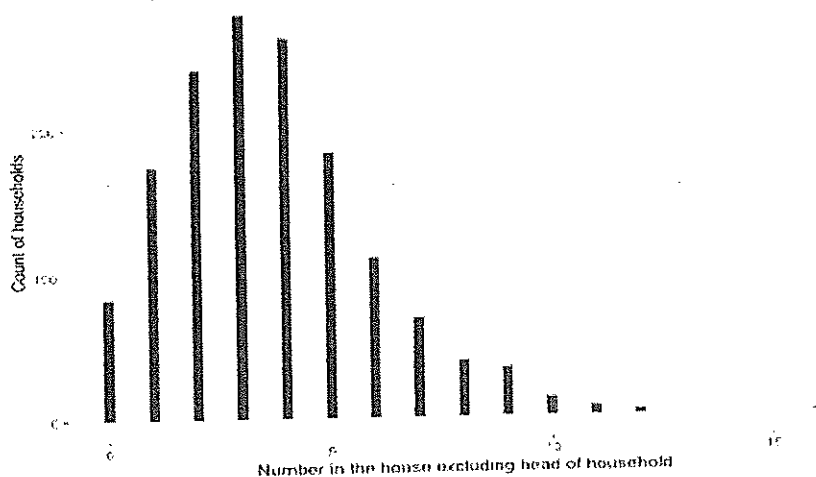
*Significant at 10%, **Significant at 5%, *** Significant at 1%

- Based on the above information, what type of model was fitted? [2]
- What was the reference category? [3]
- Comment on the model fitting information and what it means about the sufficiency of the model. [5]
- What are the assumptions of this model? Do they hold for the particular dataset? [5]
- Interpret the results of the study for both males and females. [15]

[30]

Question 3

- Suppose that the government is interested in determining the age at which heads of households in Eswatini most likely to find the largest number of people in their household. Specify the appropriate Poisson regression model for this problem. [3]
- The distribution of number of people per household is plotted below, comment on the likely distribution of the number of people per household. [4]



- Given the following array of means and variances what does the data imply in terms of the assumptions of the Poisson regression model? [6]

| Age Groups | Mean | Variance | n |
|------------|----------|-----------|-----|
| (15,20] | 1.666667 | 0.6666667 | 6 |
| (20,25] | 2.166667 | 1.5588235 | 18 |
| (25,30] | 2.918367 | 1.4098639 | 49 |
| (30,35] | 3.444444 | 2.1931464 | 108 |
| (35,40] | 3.841772 | 3.5735306 | 158 |
| (40,45] | 4.234286 | 4.4447947 | 175 |
| (45,50] | 4.489691 | 6.3962662 | 194 |
| (50,55] | 4.010638 | 5.2512231 | 188 |
| (55,60] | 3.806897 | 6.5318966 | 145 |
| (60,65] | 3.705882 | 6.1958204 | 153 |
| (65,70] | 3.339130 | 7.9980168 | 115 |
| NA | 2.549738 | 5.5435657 | 191 |

d) The following model was run using R, interpret the results.

[7]

$$\widehat{\log(\lambda)} = 1.55 - 0.0047(\text{age})$$

```
glm(formula = total ~ age, family = poisson, data = fHH1)
```

Coefficients:

```

              Estimate Std. Error z value Pr(>|z|)
(Intercept)  1.5499422   0.0502754   30.829   < 2e-16 ***
age          -0.0047059   0.0009363   -5.026 5.01e-07 ***
---

```

(Dispersion parameter for poisson family taken to be 1)

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Null deviance: 2362.5 on 1499 degrees of freedom
Residual deviance: 2337.1 on 1498 degrees of freedom
AIC: 6714

```

- e) The above model in (d) points into a situation of likely over dispersion in the model. What are the likely causes for over dispersion and what are the likely remedial measures? [5]
- f) Highlight the method of recursive least squares for testing for structural breaks in a dataset. [5]

[5]

Question 4

[30]

Figure 1 presents regressions that were estimated using data for 48 US states from 1982 – 1988 (336 observations in total). The study aimed at ascertaining the impact of socio-economic conditions and

traffic laws on the number of traffic related death accidents. Standard errors are given in parentheses under the coefficients and the p-values are given in parenthesis under the F-statistic. Maximum allowable type 1 error is 5%.

- Which is the base model? Why? [2]
- Compare and contrast the six models. [6]
- Interpret the various F statistics for the models, also comment on which model will be adequate for estimating the impact of laws and socio-economic status on traffic accidents. [8]
- Interpret the results of the model and clearly state which factors influence traffic related deaths in the US states. [10]

| Dependent Variable: Traffic Fatality Rate (Deaths Per 10,000). | | | | | | |
|---|------------------|-------------------|------------------|-----------------------|--------------------|-----------------------|
| Regressor | (1) | (2) | (3) | (4) | (5) | (6) |
| Beer tax | 0.36** (0.05) | -0.66** (0.20) | -0.64* (0.25) | -0.45* (0.22) | -0.70** (0.23) | -0.46* (0.22) |
| Drinking age 18 | | | | 0.028 (0.066) | -0.011 (0.064) | |
| Drinking age 19 | | | | -0.019 (0.040) | -0.078 (0.049) | |
| Drinking age 20 | | | | 0.031 (0.046) | -0.102* (0.036) | |
| Drinking age | | | | | | -0.002 (0.017) |
| Mandatory jail? | | | | 0.013 (0.032) | -0.026 (0.065) | |
| Mandatory community service? | | | | 0.033 (0.115) | 0.147 (0.137) | |
| Mandatory jail or community service? | | | | | | 0.031 (0.076) |
| Average vehicle miles per driver | | | | 0.008 (0.008) | 0.017 (0.010) | 0.009 (0.008) |
| Unemployment rate | | | | -0.003** (0.012) | | -0.003** (0.012) |
| Real income per capita (logarithm) | | | | 1.81** (0.47) | | 1.79** (0.45) |
| State effects? | no | yes | yes | yes | yes | yes |
| Time effects? | no | no | yes | yes | yes | yes |
| F-statistics and p-values Testing Exclusion of Groups of Variables: | | | | | | |
| Time effects = 0 | | | 2.47 (0.024) | 11.44 (<0.001) | 2.28 (0.037) | 11.59 (<0.001) |
| Drinking age coefficients = 0 | | | | 0.48 (0.696) | 2.09 (0.102) | |
| Jail, community service coefficients = 0 | | | | 0.17 (0.845) | 0.59 (0.557) | |
| Unemployment rate, income per capita = 0 | | | | 38.29 (<0.001) | | 40.12 (<0.001) |
| R ² | 0.090 | 0.889 | 0.891 | 0.926 | 0.893 | 0.926 |

Figure 1: Regression Analysis of the Effect of Drunk Laws on Traffic Deaths

- Distinguish between intrinsically linear models and non-linear models. [4]