

# **UNIVERSITY OF ESWATINI**

**FIRST SEMESTER RE-SIT EXAMINATION PAPER, SEPTEMBER 2021**

**FACULTY OF SOCIAL SCIENCES**

**DEPARTMENT OF ECONOMICS**

**COURSE CODE: ECO 419**

**TITLE OF PAPER: ECONOMETRIC METHODS I**

**TIME ALLOWED: 2 HOURS**

---

**Instructions**

1. This paper consists of Section (A) and (B).
2. Section A is compulsory.
3. Answer any two questions from Section B.

**Special Requirements**

Scientific calculator

*Candidates may complete the front cover of their answer book when instructed by the Chief Invigilator and sign their examination attendance cards but must NOT write anything else until the start of the examination period is announced.*

*No electronic devices capable of storing and retrieving text, including electronic dictionaries and any form of foreign material may be used while in the examination room.*

**DO NOT turn examination paper over until instructed to do so.**

## **SECTION A**

### **Question One (Compulsory)**

**[40 Marks]**

1. (a) Describe any 5 causes of autocorrelation. [15]

(b) Using appropriate examples, distinguish between structural and reduced form equations. [10]

(c) The following results are a computer output for testing for unit roots in real non-traditional exports of a hypothetical economy in levels (LRNTX) & differenced form (DLRNTX), respectively; where L stands for logarithm & D stands for differenced. Study the results of Test 1 below and then answer the following questions (use the DF test) :-:

(i) Are real non-traditional exports in levels stationary or nonstationary? [6]

(ii) Are differenced real non-traditional exports stationary or nonstationary? [6]

(iii) What do you think explains the difference between the results in tests 1(a) & 1(b) and those in 1(c) & 1(d)?

[3]

The Dickey-Fuller regressions include an intercept but not a trend

\*\*\*\*\*  
19 observations used in the estimation of all ADF regressions.

Sample period from 1978 to 1996

\*\*\*\*\*

	Test Statistic	LL	AIC	SBC	HQC
DF	-0.66295	.12204	-1.8780	-2.8224	-2.0378
ADF(1)	-0.52907	.12993	-2.8701	-4.2867	-3.1098
ADF(2)	-0.51075	.12997	-3.8700	-5.7589	-4.1897

\*\*\*\*\*

95% critical value for the augmented Dickey-Fuller statistic = -3.0294

#### Test 1(b) Unit root tests for variable LRNTX

The Dickey-Fuller regressions include an intercept and a linear trend

\*\*\*\*\*

19 observations used in the estimation of all ADF regressions.

Sample period from 1978 to 1996

\*\*\*\*\*

	Test Statistic	LL	AIC	SBC	HQC
DF	-2.0697	2.1712	-82878	-2.2454	-1.0685
ADF(1)	-2.2994	2.8943	-1.1057	-2.9946	-1.4254
ADF(2)	-2.6726	3.9422	-1.0578	-3.4189	-1.4573

\*\*\*\*\*

95% critical value for the augmented Dickey-Fuller statistic = -3.6746

#### Test 1(c) Unit root tests for variable DLRNTX

The Dickey-Fuller regressions include an intercept but not a trend

\*\*\*\*\*

18 observations used in the estimation of all ADF regressions.

Sample period from 1979 to 1996

\*\*\*\*\*

	Test Statistic	LL	AIC	SBC	HQC
DF	-4.2613	.089228	-1.9108	-2.8011	-2.0335
ADF(1)	-3.1113	.22791	-2.7721	-4.1076	-2.9562
ADF(2)	-2.7677	.53275	-3.4673	-5.2480	-3.7128

\*\*\*\*\*

95% critical value for the augmented Dickey-Fuller statistic = -3.0401

#### Test 1(d) Unit root tests for variable DLRNTX

The Dickey-Fuller regressions include an intercept and a linear trend

\*\*\*\*\*

18 observations used in the estimation of all ADF regressions.

Sample period from 1979 to 1996

\*\*\*\*\*

	Test Statistic	LL	AIC	SBC	HQC
DF	-4.2450	.42549	-2.5745	-3.9101	-2.7587
ADF(1)	-3.1145	.58851	-3.4115	-5.1922	-3.6570
ADF(2)	-2.6384	.77953	-4.2205	-6.4464	-4.5274

\*\*\*\*\*

95% critical value for the augmented Dickey-Fuller statistic = -3.6921

LL = Maximized log-likelihood AIC = Akaike Information Criterion

SBC = Schwarz Bayesian Criterion HQC = Hannan-Quinn Criterion

## SECTION B

**Answer any Two Questions (30 Marks Each)**

**Question Two (30 Marks)**

2. (a) What is Two-Stage Least Squares (2SLS)? [4]
- (b) Discuss the properties of 2SLS [20]
- (c) Outline 3 problems associated with differencing time series. [6]

**Question Three (30 Marks)**

3. The following 2 structural equations represent a simple demand- supply model:-

$$\text{Demand: } Q_t = a_0 + a_1 P_t + a_2 Y_t + u_{1t} \quad a_1 < 0 \quad \text{and } a_2 > 0$$

$$\text{Supply: } Q_t = b_0 + b_1 P_t + u_{2t} \quad b_1 > 0$$

Where  $Q$  is quantity,  $P$  is price, and  $Y$  is consumer's income. It is assumed that the market is cleared in every year so that  $Q_t$  represents both quantity bought and sold in year  $t$ .

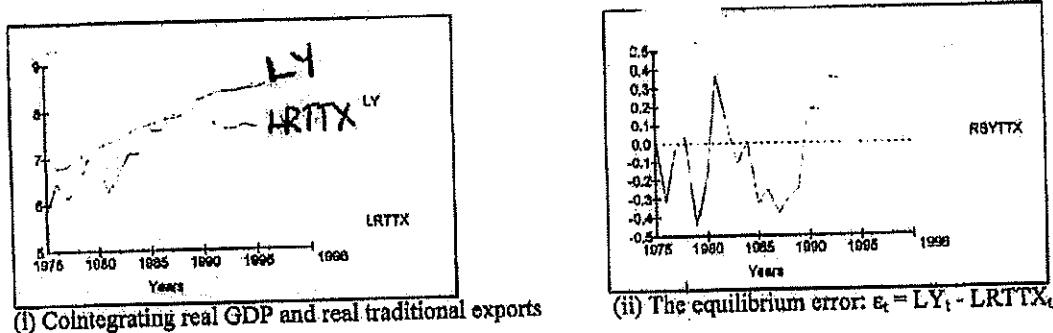
- (a) Explain why this is a simultaneous equation model? [5]
- (b) Why would the estimation of the demand & supply functions by OLS give biased and inconsistent parameter estimates? [5]
- (c) Write the reduced form equations corresponding to the structural equations. [20]

**Question Four (30 Marks)**

4. (a) What is the difference, if any, between tests of unit roots and tests of cointegration? [5]
- (b) Explain the graphical method of testing for cointegration and then indicate whether Figure 1 below, suggests that real GDP (LY) and real traditional exports (LRTTX) are cointegrated. [8]

**Figure 1**

*Cointegrating variables and their respective equilibrium errors*



(c) Consider the following equation for per capita consumption of beef in Eswatini:

$$\hat{B}_t = -330.3 + 49.1 \ln Y_t - 0.34 PB_t + 0.33 PRP_t - 15.4 D_t \dots \quad (1)$$

Se=	(7.4)	(0.13)	(0.12)	(4.1)
t=	6.6	-2.6	2.7	-3.7

$R^2 = 0.70$       n= 28      DW= 0.94

Where:  $B_t$  = the annual per capita kilograms of beef consumed in Eswatini in year t

$\ln Y_t$  = the log of real per capita disposable real income in Eswatini in year t

$PB_t$  = average annualized real wholesale price of beef in year t (in cents per kilogram)

$PRP_t$  = average annualized real wholesale price of pork in year t (in cents per kilogram)

$D_t$  = a dummy variable equal to 1 for years in which there was a “health scare” about the dangers of red meat, 0 otherwise

(i) Test for serial correlation using the Durbin–Watson d test at the 5-percent level. [6]

(d) Assume you applied the method of Generalized least squares to the estimation in (c) above and obtained the following:-

$$\hat{B}_t = -193.3 + 35.2 \ln Y_t - 0.38 PB_t + 0.10 PRP_t - 5.7 D_t \dots \quad (2)$$

Se=	(14.1)	(0.10)	(0.09)	(3.9)
$R^2$ =	0.857	n= 28	$\hat{\rho} = 0.82$	

(i) Test for serial correlation using the Durbin–Watson d test at the 5-percent level. [8]

(ii) Compare Equations 1 and 2. Which do you prefer and why? [3]

TABLE D.5A  
DURBIN-WATSON  $d$ -STATISTIC: SIGNIFICANCE POINTS OF  $d_L$  AND  $d_U$  AT 0.05 LEVEL OF SIGNIFICANCE

n	$K=1$		$K=2$		$K=3$		$K=4$		$K=5$		$K=6$		$K=7$		$K=8$		$K=9$		$k = \infty$
	$d_L$	$d_U$	$\alpha_2$																
6	0.810	1.400	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
7	0.700	1.356	0.487	1.096	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
8	0.763	1.332	0.658	1.777	0.368	2.287	—	—	—	—	—	—	—	—	—	—	—	—	—
9	0.824	1.320	0.820	1.699	0.455	2.128	0.296	2.588	—	—	—	—	—	—	—	—	—	—	—
10	0.879	1.320	0.697	1.041	0.525	2.016	0.376	2.414	0.243	2.822	—	—	—	—	—	—	—	—	—
11	0.927	1.324	0.658	1.504	0.595	1.928	0.444	2.283	0.316	2.645	0.203	3.005	—	—	—	—	—	—	—
12	0.971	1.331	0.812	1.579	0.658	1.884	0.512	2.177	0.379	2.506	0.268	2.832	0.171	3.149	—	—	—	—	—
13	1.010	1.340	0.861	1.582	0.715	1.816	0.574	2.094	0.445	2.390	0.328	2.692	0.230	2.985	0.147	3.286	—	—	—
14	1.045	1.350	0.905	1.551	0.767	1.779	0.632	2.030	0.505	2.296	0.389	2.572	0.266	2.848	0.200	3.111	0.127	3.380	—
15	1.077	1.361	0.948	1.543	0.814	1.750	0.685	1.977	0.562	2.220	0.447	2.472	0.343	2.727	0.251	2.879	0.175	3.216	0.111
16	1.108	1.371	0.982	1.539	0.857	1.728	0.734	1.936	0.616	2.157	0.502	2.388	0.398	2.624	0.304	2.860	0.222	3.090	0.155
17	1.133	1.381	1.016	1.536	0.897	1.710	0.779	1.800	0.664	2.104	0.554	2.318	0.451	2.637	0.358	2.767	0.272	2.975	0.198
18	1.158	1.391	1.046	1.535	0.933	1.696	0.820	1.872	0.710	2.060	0.603	2.257	0.502	2.481	0.407	2.667	0.321	2.873	0.244
19	1.180	1.401	1.074	1.530	0.967	1.685	0.859	1.848	0.752	2.023	0.549	2.208	0.549	2.398	0.456	2.589	0.369	2.783	0.290
20	1.201	1.411	1.100	1.537	0.998	1.676	0.894	1.828	0.792	1.981	0.692	2.162	0.595	2.339	0.502	2.621	0.416	2.704	0.336
21	1.221	1.420	1.125	1.638	1.026	1.689	0.927	1.812	0.829	1.984	0.732	2.124	0.637	2.290	0.547	2.460	0.481	2.633	0.380
22	1.239	1.429	1.147	1.541	1.053	1.684	0.958	1.797	0.883	1.940	0.769	2.090	0.677	2.246	0.588	2.407	0.504	2.571	0.424
23	1.257	1.437	1.168	1.543	1.078	1.660	0.986	1.785	0.895	1.920	0.804	2.081	0.716	2.208	0.628	2.360	0.545	2.614	0.465
24	1.273	1.448	1.188	1.546	1.101	1.656	1.013	1.775	0.925	1.902	0.837	2.035	0.751	2.174	0.666	2.318	0.584	2.464	0.508
25	1.288	1.454	1.206	1.560	1.123	1.654	1.038	1.767	0.953	1.888	0.860	2.012	0.784	2.144	0.702	2.280	0.621	2.419	0.544
26	1.302	1.461	1.224	1.653	1.143	1.652	1.062	1.759	0.979	1.873	0.897	1.992	0.816	2.117	0.735	2.246	0.657	2.379	0.581
27	1.316	1.469	1.240	1.656	1.162	1.651	1.084	1.763	1.004	1.861	0.925	1.974	0.845	2.093	0.767	2.216	0.691	2.342	0.616
28	1.328	1.476	1.255	1.660	1.181	1.650	1.104	1.747	1.028	1.850	0.951	1.958	0.874	2.071	0.798	2.188	0.723	2.309	0.650
29	1.341	1.483	1.270	1.663	1.198	1.650	1.124	1.743	1.050	1.841	0.975	1.944	0.900	2.052	0.826	2.164	0.753	2.276	0.682
30	1.352	1.489	1.284	1.567	1.214	1.650	1.143	1.739	1.071	1.833	0.998	1.931	0.926	2.034	0.854	2.141	0.782	2.261	0.712
31	1.363	1.496	1.297	1.570	1.229	1.650	1.160	1.735	1.090	1.825	1.020	1.920	0.950	2.018	0.879	2.120	0.810	2.228	0.741
32	1.373	1.502	1.309	1.674	1.244	1.650	1.177	1.782	1.109	1.819	1.041	1.909	0.972	2.004	0.904	2.102	0.838	2.203	0.769
33	1.383	1.508	1.321	1.577	1.258	1.661	1.193	1.730	1.127	1.813	1.061	1.900	0.994	1.991	0.927	2.085	0.861	2.181	0.795
34	1.393	1.514	1.333	1.600	1.271	1.662	1.208	1.728	1.144	1.808	1.080	1.891	1.015	1.979	0.950	2.088	0.885	2.182	0.821
35	1.402	1.519	1.343	1.594	1.263	1.653	1.222	1.726	1.160	1.803	1.097	1.884	1.034	1.987	0.971	2.084	0.898	2.144	0.845
36	1.411	1.525	1.354	1.667	1.295	1.654	1.238	1.724	1.175	1.799	1.114	1.877	1.053	1.957	0.991	2.041	0.930	2.127	0.888
37	1.419	1.530	1.364	1.650	1.307	1.655	1.249	1.723	1.190	1.795	1.131	1.870	1.071	1.946	1.011	2.029	0.951	2.112	0.891
38	1.427	1.535	1.373	1.654	1.318	1.656	1.281	1.722	1.204	1.792	1.146	1.864	1.088	1.939	1.029	2.017	0.970	2.090	0.912
39	1.435	1.540	1.382	1.597	1.328	1.658	1.273	1.722	1.218	1.789	1.161	1.859	1.104	1.932	1.047	2.007	0.980	2.085	0.932
40	1.442	1.544	1.391	1.600	1.329	1.659	1.295	1.721	1.230	1.786	1.175	1.864	1.120	1.924	1.064	1.997	1.008	2.072	0.952
45	1.476	1.566	1.430	1.615	1.383	1.666	1.336	1.720	1.287	1.776	1.238	1.835	1.189	1.895	1.139	1.858	1.089	2.022	1.036
50	1.503	1.585	1.482	1.628	1.421	1.674	1.378	1.721	1.335	1.771	1.291	1.822	1.246	1.875	1.201	1.930	1.158	1.986	1.110
55	1.528	1.601	1.490	1.621	1.452	1.681	1.414	1.724	1.374	1.768	1.334	1.814	1.294	1.861	1.253	1.909	1.212	1.950	1.170
60	1.549	1.616	1.514	1.652	1.460	1.669	1.444	1.727	1.400	1.767	1.372	1.808	1.335	1.850	1.298	1.894	1.260	1.939	1.222
65	1.567	1.629	1.536	1.602	1.503	1.696	1.471	1.731	1.438	1.787	1.404	1.805	1.370	1.843	1.338	1.882	1.301	1.923	1.268
70	1.583	1.641	1.554	1.672	1.525	1.703	1.494	1.735	1.464	1.768	1.433	1.802	1.401	1.837	1.369	1.873	1.337	1.910	1.305
75	1.598	1.652	1.571	1.600	1.543	1.709	1.515	1.739	1.487	1.770	1.458	1.801	1.428	1.834	1.399	1.867	1.369	1.901	1.339
80	1.611	1.662	1.596	1.608	1.560	1.716	1.534	1.743	1.507	1.772	1.480	1.801	1.453	1.831	1.425	1.861	1.397	1.893	1.369
85	1.624	1.671	1.600	1.696	1.575	1.721	1.550	1.747	1.625	1.774	1.500	1.801	1.474	1.829	1.448	1.857	1.422	1.886	1.398
90	1.635	1.679	1.612	1.703	1.589	1.726	1.566	1.751	1.642	1.776	1.518	1.801	1.494	1.827	1.469	1.854	1.445	1.881	1.420
95	1.645	1.687	1.623	1.708	1.602	1.732	1.579	1.755	1.567	1.778	1.535	1.802	1.512	1.827	1.489	1.852	1.465	1.877	1.442
100	1.654	1.694	1.634	1.715	1.613	1.736	1.592	1.758	1.571	1.780	1.550	1.803	1.528	1.826	1.508	1.850	1.484	1.874	1.462
150	1.720	1.746	1.706	1.760	1.693	1.774	1.679	1.780	1.665	1.802	1.651	1.817	1.637	1.832	1.622	1.847	1.608	1.862	1.594
200	1.758	1.776	1.748	1.789	1.736	1.769	1.728	1.810	1.718	1.820	1.707	1.831	1.697	1.841	1.686	1.852	1.675	1.863	1.674

n	K' = 11		K' = 12		K' = 13		K' = 14		K' = 15		K' = 16		K' = 17		K' = 18		K' = 19		K' = 20		
	d <sub>L</sub>	d <sub>U</sub>																			
16	0.090	3.503	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
17	0.138	3.378	0.087	3.557	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
18	0.177	3.285	0.123	3.441	0.078	3.603	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
19	0.220	3.159	0.160	3.335	0.111	3.496	0.070	3.642	—	—	—	—	—	—	—	—	—	—	—	—	—
20	0.263	3.063	0.200	3.234	0.145	3.395	0.100	3.542	0.063	3.676	—	—	—	—	—	—	—	—	—	—	—
21	0.307	2.978	0.240	3.141	0.192	3.300	0.132	3.448	0.091	3.583	0.058	3.705	—	—	—	—	—	—	—	—	—
22	0.349	2.897	0.281	3.057	0.220	3.211	0.168	3.358	0.120	3.495	0.083	3.619	0.052	3.731	—	—	—	—	—	—	—
23	0.381	2.826	0.322	2.979	0.259	3.128	0.202	3.272	0.163	3.409	0.110	3.635	0.076	3.850	0.048	3.753	—	—	—	—	—
24	0.431	2.761	0.362	2.908	0.287	3.053	0.239	3.193	0.186	3.327	0.141	3.464	0.101	3.672	0.070	3.678	0.044	3.773	—	—	—
25	0.470	2.702	0.400	2.844	0.335	2.983	0.276	3.119	0.221	3.251	0.172	3.376	0.130	3.494	0.094	3.604	0.065	3.702	0.041	3.700	—
26	0.508	2.649	0.439	2.784	0.379	2.919	0.312	3.051	0.259	3.179	0.205	3.303	0.160	3.420	0.120	3.531	0.087	3.632	0.060	3.724	—
27	0.544	2.600	0.475	2.730	0.409	2.859	0.348	2.987	0.281	3.112	0.238	3.233	0.181	3.349	0.149	3.460	0.112	3.563	0.081	3.656	—
28	0.578	2.555	0.510	2.680	0.445	2.805	0.383	2.928	0.326	3.050	0.271	3.168	0.222	3.283	0.178	3.392	0.138	3.485	0.104	3.692	—
29	0.612	2.515	0.544	2.634	0.479	2.755	0.418	2.874	0.359	2.992	0.305	3.107	0.254	3.219	0.208	3.327	0.166	3.431	0.129	3.628	—
30	0.643	2.477	0.577	2.592	0.512	2.708	0.451	2.823	0.392	2.937	0.337	3.050	0.288	3.160	0.238	3.268	0.195	3.368	0.156	3.465	—
31	0.674	2.443	0.608	2.553	0.545	2.668	0.484	2.778	0.425	2.887	0.370	2.990	0.317	3.103	0.269	3.208	0.224	3.309	0.183	3.406	—
32	0.703	2.411	0.638	2.517	0.576	2.626	0.615	2.733	0.457	2.840	0.401	2.946	0.348	3.050	0.299	3.153	0.253	3.262	0.211	3.348	—
33	0.731	2.382	0.668	2.484	0.608	2.588	0.546	2.692	0.488	2.798	0.432	2.899	0.378	3.000	0.329	3.100	0.283	3.198	0.239	3.293	—
34	0.758	2.355	0.695	2.454	0.634	2.654	0.575	2.654	0.518	2.754	0.482	2.854	0.409	2.954	0.359	3.051	0.312	3.147	0.267	3.240	—
35	0.783	2.330	0.722	2.425	0.662	2.521	0.604	2.619	0.547	2.718	0.492	2.813	0.439	2.910	0.388	3.005	0.340	3.099	0.295	3.190	—
36	0.808	2.306	0.748	2.308	0.689	2.402	0.631	2.588	0.576	2.680	0.620	2.774	0.467	2.868	0.417	2.961	0.389	3.053	0.323	3.142	—
37	0.831	2.285	0.772	2.374	0.714	2.464	0.657	2.655	0.602	2.646	0.548	2.738	0.495	2.829	0.445	2.920	0.387	3.008	0.351	3.097	—
38	0.876	2.248	0.819	2.329	0.763	2.413	0.707	2.499	0.653	2.685	0.600	2.671	0.549	2.757	0.499	2.843	0.451	2.929	0.404	3.054	—
39	0.898	2.228	0.840	2.309	0.785	2.391	0.731	2.473	0.678	2.557	0.628	2.641	0.575	2.724	0.525	2.808	0.477	2.892	0.430	2.974	—
40	0.904	2.198	0.938	2.225	0.887	2.288	0.838	2.367	0.788	2.439	0.740	2.512	0.692	2.588	0.644	2.659	0.598	2.733	0.553	2.807	—
45	1.231	2.008	1.195	2.049	1.160	2.093	1.124	2.138	1.088	2.183	1.052	2.229	1.016	2.276	0.980	2.323	0.944	2.371	0.908	2.419	—
50	1.129	2.082	1.087	2.116	1.045	2.170	1.003	2.225	0.981	2.281	0.919	2.338	0.877	2.386	0.838	2.454	0.798	2.512	0.764	2.571	—
60	1.184	2.031	1.145	2.079	1.108	2.127	1.068	2.177	1.029	2.227	0.980	2.278	0.951	2.330	0.913	2.382	0.874	2.434	0.838	2.487	—
65	1.272	1.980	1.239	2.026	1.208	2.068	1.172	2.106	1.139	2.148	1.105	2.189	1.072	2.232	1.038	2.275	1.005	2.318	0.971	2.382	—
75	1.308	1.970	1.277	2.008	1.247	2.043	1.215	2.080	1.184	2.118	1.153	2.166	1.121	2.195	1.090	2.235	1.058	2.275	1.027	2.315	—
80	1.340	1.957	1.311	1.981	1.283	2.024	1.253	2.059	1.224	2.093	1.195	2.129	1.165	2.185	1.136	2.201	1.106	2.238	1.076	2.275	—
85	1.369	1.946	1.342	1.977	1.315	2.009	1.287	2.040	1.260	2.073	1.232	2.105	1.205	2.139	1.177	2.172	1.149	2.206	1.121	2.241	—
90	1.395	1.937	1.369	1.966	1.344	1.995	1.318	2.025	1.292	2.055	1.266	2.085	1.240	2.116	1.213	2.148	1.187	2.179	1.160	2.211	—
95	1.416	1.929	1.394	1.958	1.370	1.984	1.345	2.012	1.321	2.040	1.296	2.068	1.271	2.097	1.247	2.128	1.222	2.156	1.197	2.186	—
100	1.439	1.923	1.416	1.948	1.393	1.974	1.371	2.000	1.347	2.028	1.324	2.053	1.301	2.080	1.277	2.108	1.263	2.135	1.229	2.164	—
150	1.579	1.892	1.664	1.908	1.650	1.924	1.635	1.940	1.619	1.956	1.604	1.972	1.689	1.989	1.474	2.006	1.458	2.023	1.443	2.040	—
200	1.654	1.885	1.643	1.890	1.632	1.908	1.621	1.919	1.610	1.931	1.609	1.943	1.588	1.965	1.578	1.967	1.585	1.979	1.554	1.991	—

Source: This table is an extension of the original Durbin-Watson table and is reproduced from N. E. Savin and K. J. White, "The Durbin-Watson Test for Serial Correlation with Extreme Small Samples of Many Regressors," *Econometrica*, vol. 45, November 1977, pp. 1089-96 and as corrected by R. W. Farebrother.

Note: n = number of observations, K' = number of explanatory variables excluding the constant term.