

University of Eswatini

Department of Chemistry

November 2018 Main Examination

TITLE OF PAPER : Introduction to Thermodynamics

COURSE NUMBER : CHE 241

TIME : 3 Hours

- Important Information**
- : Each question is equivalent to 25% of the entire exam.
 - : Answer **questions one (1) and any other three (3)** questions in this paper.
 - : Marks for ALL procedural calculations will be awarded.
 - : Start each question on a fresh page of the answer sheet.
 - : Diagrams must be large and clearly labelled accordingly.
 - : Additional material: data sheet, graph paper and the periodic table.

You are not supposed to open this paper until permission has been granted by the Chief Invigilator

Question 1: Compulsory [25 Marks]

The compressibility factor, X, for a real gas is given by

$$Z = \frac{PV}{nRT}$$

- a) Use the following data to plot Z versus P for O₂ at 273 K

P (atm)	1	100	200	300	500	700	900
V _m (L.mol ⁻¹)	22.41	0.2077	0.1024	0.0719	0.0518	0.0444	0.0403

- b) Using the data in (a), compare and contrast real gases and ideal gases [10]
- c) The behaviour of gaseous Naphthalene (C₁₀H₈) follows the Van der Waals equation of state. Given that at 100°C, C₁₀H₈ expands isothermally and reversibly from 20 dm³ to 60 dm³, calculate w, q and ΔU. [15]
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Question 2 [25 Marks]

- a) Write short notes on the following;

- i. Enthalpy change [2]
ii. Hess's law [2]

- b) Calculate the standard enthalpies of formation of:

- i. KClO₃ from the enthalpy of formation of KCl [4]
ii. NOCl from the enthalpy of formation of NO; given the attached table and the following information; [4]



- c) Outline the Carnot cycle using a P-V diagram explaining all its stages and associated energy changes and conditions for each step. [6]

- d) A heat engine absorbs 2500J of heat and discards 2100J. Calculate the work performed by the engine and its maximum efficiency. [7]
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Question 3 [25 Marks]

- a) Write short notes on the heat capacity and show how it links with ΔH as well as q_v . [10]
- b) The enthalpy of vaporization of bromine is 30.9 kJ/mol and the standard entropy values of liquid and gaseous bromine are 152 J/mol and 245 J/molK. Estimate the boiling point of bromine [10]
- c) Show graphically, the differences between an endothermic system and an exothermic system [5]
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Question 4 [25 Marks]

- a) A Carnot engine takes 4500 J of heat energy from a reservoir at 800 K.
- How much heat will be released to a cold reservoir at 27°C? [4]
 - Calculate the amount of work performed by this engine. [3]
 - What is the Carnot efficiency of this engine [3]
- b) Methanol boils at 64.1°C and its enthalpy of vaporization is 35.27 kJmol⁻¹. Calculate;
- The entropy of vaporization at these conditions, [5]
 - The entropy change of the surroundings. [5]
- c) Write short notes on the following;
- Nernst heat theorem [2]
 - Standard molar entropy [3]
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Question 5 [25 marks]

- a) Two empirical equations of state are the Dieterici and the van der Waals equations. Derive the critical constants for both equations of state [15]
- b) Write notes on surface tension, include diagrams and examples where necessary [10]
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Question 6 [25 marks]

- a) To calibrate a calorimeter, 0.120 g naphthalene ($C_{10}H_8$) was burnt at constant volume and it caused the temperature of the calorimeter to rise by $3.05\text{ }^{\circ}\text{C}$. Then 0.10g of unknown compound was burned in the same calorimeter, causing a temperature rise of $2.05\text{ }^{\circ}\text{C}$.
- i. Calculate the heat capacity of calorimeter [5]
 - ii. Is the unknown compound phenol, $C_6H_5OH(s)$ or ethanol, $CH_3CH_2OH(l)$ whose enthalpies of combustion are $\Delta_C H^\Theta = 3054\text{ kJmol}^{-1}$ and -1368 kJmol^{-1} , respectively [6]
- b) Compare and contrast;
- i. Reversible and irreversible expansion [5]
 - ii. Path and state functions [4]
 - iii. Change in internal energy and change in enthalpy [5]

The End

Standard molar Gibbs free energy and molar entropy of formation at 298.15 K

M _T	ΔG _f ^θ /kJ/mol	S _f ^θ /J K ⁻¹ mol ⁻¹	M _T	ΔG _f ^θ /kJ/mol	S _f ^θ /J K ⁻¹ mol ⁻¹
H ₂ O(g)	18.015	-228.57	188.83	O ₂ (g)	47.998
H ₂ O(l)	18.015	-120.35	109.6	NO(g)	30.006
H ₂ O(l)	34.015	-120.35	109.6	NO(g)	46.006
NH ₃ (g)	17.031	-16.45	192.45	N ₂ O ₄ (g)	92.012
NH ₃ (l)	32.045	149.43	121.21	SO ₂ (g)	64.063
NH ₃ (l)	43.028	327.3	140.6	H ₂ S(g)	34.080
NH ₃ (g)	43.028	328.1	238.97	SF ₆ (g)	146.054
HNO ₃ (l)	63.013	-80.71	155.60	HCl(g)	20.006
NH ₄ OH(g)	33.030			HCl(g)	36.461
NH ₄ Cl(s)	53.492	-202.87	94.6	HCl(aq)	36.461
HgCl ₂ (s)	271.50	-178.6	146.0	HBr(g)	80.917
H ₂ SO ₄ (aq)	98.078	-690.00	156.90	H(g)	127.912
H ₂ SO ₄ (aq)	98.078	-744.53	20.1	CO(g)	44.010
NaCl(s)	58.443	-384.14	72.13	CO ₂ (g)	28.011
NaOH(s)	39.997	-379.49	64.46	Al ₂ O ₃ (s)	101.945
KCl(s)	74.555	-409.14	82.59	SiO ₂	60.09
KBr(s)	119.011	-380.66	95.90	FeS(s)	87.91
KI(s)	166.006	-324.89	106.32	FeS(s)	119.975
He(g)	4.003	0	126.15	He(g)	200.59
Ar(g)	39.95	0	154.84	He(l)	200.59
H ₂ (g)	2.016	0	130.684	Ag(g)	107.87
N ₂ (g)	28.013	0	191.61	Ag(s)	107.87
O ₂ (g)	31.999	0	205.138	Na(g)	370.95
O ₃ (g)	47.998	163.2	228.93	Na(s)	22.99
Cl ₂ (g)	70.91	0	223.07		0
Br ₂ (g)	159.82	3.110	245.46		
Br ₂ (l)	159.82	0	152.23		
I ₂ (g)	253.81	19.33	260.69		
I ₂ (s)	253.81	0	116.135		
organic compounds					
CH ₄ (g) methane				16.043	-50.72
C ₂ H ₂ (g) ethyne				20.038	209.20
C ₂ H ₄ (g) ethene				28.05	68.15
C ₂ H ₆ (g) ethane				30.070	-32.82
C ₃ H ₆ cyclopropane(g)				42.081	104.45
C ₃ H ₆ propane(g)				42.031	62.78
C ₄ H ₁₀ n-butane(g)				58.124	-17.03
C ₅ H ₁₂ n-pentane(g)				72.151	-8.20
C ₆ H ₁₂ cyclohexane(l)				84.163	26.8
C ₆ H ₁₄ n-hexane(l)				86.178	204.3
C ₆ H ₆ benzene(l)				78.115	124.3
C ₆ H ₆ benzene(g)				78.115	129.72
C ₈ H ₁₈ n-octane(l)				114.233	6.4
C ₁₀ H ₈ naphthalene(l)				128.175	361.1
CH ₃ OH(g)				32.042	-161.96
CH ₃ OH(l)				32.042	-166.27
CH ₃ CHO(g)				44.054	-128.86
CH ₃ CH ₂ OH(l)				46.07	-174.78
CH ₃ COOH(l)				60.053	-389.9
CH ₃ COOC ₂ H ₅ (l)				88.107	-332.7
C ₆ H ₅ OH(s)				94.114	259.4
C ₆ H ₅ NH ₂ (l)				93.129	159.8
CH ₂ (NH ₂)CO ₂ H glycine(s)				75.068	-373.4
C ₆ H ₁₂ O ₆ , D-D-Glucose(s)				180.159	103.5
C ₆ H ₂₂ O ₁₁ , sucrose(s)				180.159	212
CH ₃ CH(OH)COOH				90.079	-1543
lactic acid(s)					360.2

Source: American Institute of Physics handbook, McGraw-Hill.

Standard molar enthalpies of formation at 298.15 K

Temperature dependence of heat capacities, $C_{p,m} = a + bT + cT^2$

	M_r	$\Delta H_f^\theta / \text{kJ/mol}$		M_r	$\Delta H_f^\theta / \text{kJ/mol}$	$a/10^3 \text{ K}^{-1} \text{ mol}^{-1}$	$b/10^{-3} \text{ J}^{-2} \text{ mol}^{-1}$	$c/10^5 \text{ J K mol}^{-1}$
$\text{H}_2\text{O(l)}$	18.015	-241.8	$\text{O}_3(\text{g})$	47.993	+142.7			
$\text{H}_2\text{O(g)}$	18.015	-205.8	NO(g)	30.006	+90.2	$\text{He}, \text{Ne}, \text{Ar}, \text{Kr}, \text{Xe}$	20.78	0
$\text{H}_2\text{O}_2(\text{l})$	34.015	-187.8	$\text{NO}_2(\text{g})$	46.006	+33.2	H_2	27.28	3.26
$\text{NH}_3(\text{g})$	17.031	-48.1	$\text{N}_2\text{O}_4(\text{g})$	92.012	+9.2	O_2	29.98	4.18
$\text{NH}_4(\text{l})$	32.045	+50.6	$\text{SO}_3(\text{g})$	64.063	-296.8	N_2	28.58	3.77
$\text{NH}_4(\text{l})$	43.028	+284.1	$\text{H}_2\text{S(g)}$	34.080	-20.6	Cl_2	37.03	0.67
$\text{NH}_3(\text{g})$	43.028	+294.1	$\text{SF}_6(\text{g})$	148.054	-120.9	CO_2	44.23	6.79
$\text{HNO}_3(\text{l})$	63.013	-174.1	HF(g)	20.056	-271.1	H_2O	30.54	10.28
$\text{NH}_2\text{OH(s)}$	33.030	-114.2	HCl(g)	38.461	-92.3	NH_3	28.75	25.10
$\text{NH}_4\text{Cl(s)}$	53.492	-314.4	HCl(aq)	36.461	-167.2	CH_4	23.64	47.86
$\text{HgCl}_2(\text{s})$	271.50	-224.3	HBr(g)	80.917	+36.4			-1.92
$\text{H}_2\text{SO}_4(\text{l})$	98.078	-814.0	HI(g)	127.912	+26.5			0.82
$\text{H}_2\text{SO}_4(\text{aq})$	98.078	-99.3	$\text{CO}_2(\text{g})$	44.010	-383.5			0
NaCl(s)	58.443	-411.0	CO(g)	26.011	-110.5			-1.5
NaOH(s)	39.987	-428.7	$\text{Al}_2\text{O}_3(\text{s})$	101.945	-1675.7			-1.92
KCl(s)	74.555	-435.8	$\text{SiO}_2(\text{s})$	60.085	-910.9			
KBr(s)	119.011	-392.2	FeS(s)	87.91	-100.0			
$\text{K}_2\text{SO}_4(\text{s})$	165.006	-327.6	$\text{FeS}_2(\text{s})$	118.975	-178.2			
Diatomics(g)	—	0	AgCl(s)	143.323	-127.1	$\text{CH}_4(\text{g})$	16.043	1580
						$\text{C}_2\text{H}_2(\text{g})$	26.038	2058
						$\text{C}_2\text{H}_4(\text{g})$	28.054	2877
						$\text{C}_2\text{He(g)}$	30.070	3336
						$\text{C}_3\text{He-cyclopropane(g)}$	42.081	3202
						$\text{C}_3\text{He-propene(g)}$	53.35	4183
						$\text{C}_4\text{H}_{10-n-butane(g)}$	58.124	5157
						$\text{C}_5\text{H}_{12-n-pentane(g)}$	72.151	5471
						$\text{C}_6\text{H}_{12-cyclohexane(g)}$	84.183	588.0
						$\text{C}_8\text{H}_{14-n-hexane(g)}$	86.178	726.1
						$\text{C}_6\text{He-benzene(l)}$	78.115	1183
						$\text{C}_8\text{H}_{18-n-octane(l)}$	114.233	1398
						$\text{C}_{10}\text{He-naphthalene(l)}$	128.175	184.2
						$\text{CH}_3\text{OH(l)}$	32.042	874.5
						$\text{CH}_3\text{CHO(g)}$	44.034	2021
						$\text{CH}_3\text{CH}_2\text{OH(l)}$	46.070	246.6
						$\text{CH}_3\text{COOH(l)}$	60.053	3054
						$\text{CH}_3\text{COOC}_2\text{H}_5(\text{l})$	88.107	333.0
						$\text{CH}_2(\text{NH}_2)\text{CO}_2\text{H}_2, \text{glycine(s)}$	75.083	632.2
						$\text{C}_6\text{H}_{12}\text{O}_5-\alpha\text{-D-glucose(s)}$	180.159	984.4
						$\text{C}_6\text{H}_{12}\text{O}_5-\beta\text{-D-glucose(s)}$	180.159	2808
						$\text{C}_12\text{H}_{22}\text{O}_{11}-\text{succrose(s)}$	342.303	5845
						$\text{CH}_3\text{CH}_2\text{OHCOOH}$	90.079	1344
						lactic acid(s)	694.0	

^a: Sublimation; ^b: various pressures; ^c: at 1 atm

Source: American Institute of Physics handbook, McGraw-Hill

Heat capacities at 25°C

	C _{v,m} JK ⁻¹ mol ⁻¹	C _{p,m} JK ⁻¹ mol ⁻¹
He, Ne, Ar, Kr, Xe	12.47	20.78
H ₂	20.50	28.81
O ₂	21.01	29.33
N ₂	20.83	29.14
CO ₂	28.83	37.14
NH ₃	27.17	35.48
CH ₄	27.43	35.74
N ₂ O		77.28
NO ₂		37.20

F.P Depression, B.P. Elevation

Solvent	F.P °C	K _f °C kg mol ⁻¹ (°C, 10 kNm ⁻²)	B.P °C kg mol ⁻¹	K _b °C kg mol ⁻¹
Water	0	1.86	100.0	0.52
Benzene	5.51	5.10	80.1	2.60
Acetic Acid	16.6	3.90	118.1	3.10
Cyclohexane	6.5	20.2	81.4	2.79
Camphor	177.7	40.0	205	-
Nitrobenzene	5.7	6.9	210.9	5.24
Ethanol	-1.77		78.5	1.22
Chlooreform	-64		61.3	3.63

Third Law entropies at 25°C, Sm^θ/J K⁻¹ mol⁻¹

Solids	Liquids			Gases	
Ag	42.68	Hg	76.02	H ₂	130.6
Cl _(g)	5.77	Br ₂	152.3	N ₂	192.1
Cl _(d)	2.44			O ₂	205.1
Cu	33.4			Cl ₂	223.0
Zn	41.6	H ₂ O	70.0	CO	197.67
H ₂	116.7			CO ₂	213.7
S(Rh)	31.9	HNO ₃	155.6	HCl	186.8
				H ₂ S	205.6
AgCl	96.2	C ₂ H ₅ OH	161.0	NH ₃	192.5
AgBr	104.6	CH ₃ OH	126.7	CH ₄	186.1
CuSO ₄ ·5H ₂ O	305.4	C ₆ H ₆	49.03	C ₂ H ₆	229.4
HgCl ₂	144	CH ₃ COOH	159.8	CH ₃ CHO	265.7
Sucrose	360.2	C ₆ H ₁₂	298.2		

<u>Useful Relations</u>		General Data						
$(RT)_{298.15K} = 2.4789 \text{ kJ/mol}$		speed of light	$c = 2.997925 \times 10^8 \text{ ms}^{-1}$					
$(RTF)_{298.15K} = 0.025693 \text{ V}$		charge of proton	$e = 1.60219 \times 10^{-19} \text{ C}$					
T/K:	100.15 298.15 500.15 1000.15	Faraday constant	$F=L e = 9.64846 \times 10^4 \text{ C mol}^{-1}$					
T/Cm ⁻¹ :	69.61 207.22 347.62 695.13	Boltzmann constant	$k = 1.38066 \times 10^{-23} \text{ J K}^{-1}$					
1mmHg=133.222 N m ⁻²		Gas constant	$R=Lk = 8.31441 \text{ J K}^{-1} \text{ mol}^{-1}$					
$\hbar/c = 1.43878 \times 10^{-2} \text{ m K}$			$8.20575 \times 10^{-2} \text{ dm}^3 \text{ atm K}^{-1} \text{ mol}^{-1}$					
1atm	1 cal	1 eV	1 cm ⁻¹					
= $1.01325 \times 10^5 \text{ N m}^{-2}$	= 4.184 J	= $1.602189 \times 10^{-19} \text{ J}$	= $-0.124 \times 10^{-3} \text{ eV}$					
=760torr		= 96.485 kJ/mol	= $1.9864 \times 10^{-23} \text{ J}$					
=1 bar		= 8065.5 cm^{-1}						
SI-units:								
$IL = I000 ml = 1000 cm^3 = 1 dm^3$		Avogadro constant	$L \text{ or } N_A = 6.02214 \times 10^{23} \text{ mol}^{-1}$					
1 dm = 0.1 m		Atoms mass unit	$u = 1.66054 \times 10^{-27} \text{ kg}$					
1 cal (thermochemical) = 4.184 J		Electron mass	$m_e = 9.10939 \times 10^{-31} \text{ kg}$					
dipole moment: 1 Debye = $3.33564 \times 10^{-30} \text{ C m}$		Proton mass	$m_p = 1.67262 \times 10^{-27} \text{ kg}$					
force: $IN = IJ m^{-1} = I kgms^{-2} = 10^3 \text{ dyne}$ pressure: $IPa = INm^{-2} = 1 J m^{-3}$		Neutron mass	$m_n = 1.67493 \times 10^{-27} \text{ kg}$					
$IJ = INm$		Vacuum permittivity	$\epsilon_0 = \mu_0^{-1} c^{-2} = 8.854188 \times 10^{-12} \text{ J}^{-1} \text{ C}^{-2} \text{ m}^{-1}$					
power: $1W = 1J s^{-1}$		Vacuum permeability	$\mu_0 = 4\pi \times 10^{-7} \text{ Js}^2 \text{ C}^{-2} \text{ m}^{-1}$					
potential: $1V = 1J C^{-1}$		Bohr magneton	$\mu_B = e\hbar/2m_e = 9.27402 \times 10^{-24} \text{ JT}^{-1}$					
magnetic flux: $1T = 1Vs m^{-2} = 1ICsm^{-2}$		Nuclear magneton	$\mu_N = e\hbar/2m_p = 5.05079 \times 10^{-27} \text{ JT}^{-1}$					
current: $1A = 1Cs^{-1}$		Gravitational constant	$G = 6.67259 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2}$					
Prefixes:		Gravitational acceleration	$g = 9.80665 \text{ ms}^{-2}$					
P n m m d k M G		Bohr radius	$a_0 = 5.29177 \times 10^{-11} \text{ m}$					
pico nano micro milli centi deci kilo mega giga								
10^{-12}	10^{-9}	10^{-6}	10^{-3}	10^{-2}	10^{-1}	10^3	10^6	10^9

THE PERIODIC TABLE OF ELEMENTS

Group	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
Period	1	IA	IIA	IIIB	IVB	VB	VIB	VIB	VIB	VIB	VIIA	IB	IB	IIA	IVA	VA	VIA	VIIA
1	H 1.008																	
2	Li 6.94	Be 9.01																
3	Na 22.99	Mg 24.31																
4	K 39.10	Ca 40.08	Sc 44.96	Ti 47.90	V 50.94	Cr 52.01	Mn 54.9	Fe 55.85	Co 58.71	Ni 58.71	Cu 63.54	Zn 65.37	Ga 69.7	Ge 72.59	As 74.92	Se 78.96	Br 79.91	Kr 83.80
5	Rb 85.47	Sr 87.62	Y 88.91	Zr 91.22	Nb 91.22	Mo 95.94	Tc 98.9	Ru 101.1	Rh 102.9	Pd 106.4	Ag 107.9	Cd 112.4	In 114.8	Sn 118.7	Sb 121.8	Te 127.6	I 126.9	Xe 131.3
6	Cs 132.9	Ba 137.3	Lu 174.9	Hf 178.5	Ta 180.9	W 183.8	Re 186.2	Os 190.2	Ir 192.2	Pt 195.1	Au 196.9	Hg 200.6	Tl 204.4	Pb 207.2	Bi 208.9	Po 210	At 210	Rn 222.1
7	Fr 223	Ra 226.0	Lr 257	Unq	Unp	Unh	Uns	Uno	Une									
Lanthanides			La 138.9	Ce 140.1	Pr 140.9	Nd 144.2	Pm 146.9	Sm 150.9	Eu 151.3	Gd 157.3	Tb 158.9	Dy 162.5	Ho 164.9	Er 167.3	Tm 168.9	Yb 173.0		
Actinides			Ac 227.0	Th 232.0	Pa 231.0	U 238.0	Np 237.1	Pu 239.1	Am 241.1	Cm 247.1	Bk 249.1	Cf 251.1	Fm 254.1	Md 257.1	No 258.1			

Numbers below the symbol indicates the atomic masses; and the numbers above the symbol indicates the atomic numbers;

SOURCE: International Union of Pure and Applied Chemistry, I. Mills, ed., *Quantities, Units, and Symbols in Physical Chemistry*, Blackwell Scientific Publications, Boston, 1988, pp 86-98.