

UNIVERSITY OF SWAZILAND
MAIN EXAMINATION PAPER 2008/2009

TITLE OF PAPER: **BIOSTATISTICS**

COURSE CODE: **B305**

TIME ALLOWED: **THREE (3) HOURS**

- INSTRUCTIONS:**
1. **ANSWER ANY FOUR QUESTIONS.**
 2. **EACH QUESTION CARRIES TWENTY FIVE (25) MARKS.**
 3. **ILLUSTRATE YOUR ANSWERS WITH LARGE AND CLEARLY LABELED DIAGRAM WHERE APPROPRIATE.**
 4. **CLEARLY STATE YOUR NULL AND ALTERNATIVE HYPOTHESES AND YOUR CONCLUSIONS WHERE APPROPRIATE.**

SPECIAL REQUIREMENTS:

1. **CALCULATORS (CANDIDATES MUST BRING THEIR OWN).**
2. **GRAPH PAPER.**
3. **STATISTICAL TABLES (TO BE SUPPLIED BY THE LECTURER).**

THIS PAPER IS NOT TO BE OPENED UNTIL PERMISSION HAS BEEN GRANTED BY THE INVIGILATORS

ANSWER ANY FOUR (4) OUT OF THE SIX (6) QUESTIONS**QUESTION 1**

The following mortality data were collected for a particular species of plant. A total of 163 saplings were followed until their death. The number present under the "survival" column refers to the number of plants dying in that particular age group (out of the total of 163 individual plants).

Mortality	Age group (years)
130	<1
30	1
10	2
10	3
8	4
7	5
6	6
7	7
5	8
5	9
Total = 218	

- a) Calculate the mortality rate associated with each age group and present it as a percentage

[5 marks]

- b) Present these data graphically.

[10 marks]

- c) What are the essential components of a research proposal?

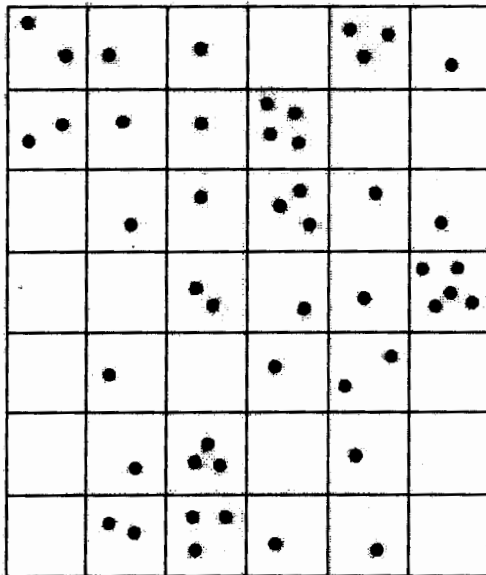
[10 marks]

[TOTAL = 25 marks]**QUESTION 2**

Consider the distribution of rodent burrows (see map on next page). Each dot represents a burrow. Are the burrows distributed randomly in the habitat?

QUESTION 2 (continued)

Distribution of rodent burrows in a natural habitat.



[TOTAL = 25 marks]

QUESTION 3

The following table shows the number of ectoparasites in a sample of marine turtles at several Indian Ocean islands. The data are **NOT** normally distributed.

Number of ectoparasites in marine turtles			
Mauritius	Comores	Seychelles	Reunion
6	5	5	8
5	4	4	7
4	4	3	8
5	3	5	6
3	6	6	7
4	5	6	8

QUESTION 3 (continued)

Using an **appropriate** statistical test, establish whether turtles in the four different regions have significantly different amounts of ectoparasites.

[TOTAL = 25 marks]

QUESTION 4

The following data were collected by an ecologist studying the foraging movements of nocturnal primates in a tropical forest:

Mean distance from roost (m)	Body mass (g)
1500	600
700	200
650	150
645	120
832	280
500	80
651	180
347	50
350	80
352	60

- a) Which are the dependent and independent variables? [2 marks]
- b) Calculate a and b for the regression of travel distance on body mass. [15 marks]
- c) Is there a significant relationship between travel distance and body mass? Use an **appropriate** statistical test to support your answer. [8 marks]

[TOTAL = 25 marks]

QUESTION 5

- a) What is the difference between a histogram, box plot and an x-y graph?

[5 marks]

QUESTION 5 (continued)

- b) Consider the data in the table in Question 6 (next question). Present these data graphically, using an appropriate graph. [10 marks]
- c) How can you ensure that your experimental design is appropriate and robust? [10 marks]
- [TOTAL = 25 marks]

QUESTION 6

Consider the following data on aquatic invertebrates exposed to different levels of pollution in different climatic regions.

Climatic region	Numbers		
	Polluted stream	Slightly polluted	Unpolluted stream
Hot/wet	23	38	65
Hot/dry	15	22	45
Cool/wet	16	25	42
Cool/dry	10	18	35

- a) Are the numbers of aquatic invertebrates evenly distributed across polluted habitats in the different climatic regions? Use chi-square to test this. [17 marks]
- b) What are the assumptions of the chi-square test? [4 marks]
- c) What are the assumptions of the t-test? [4 marks]
- [TOTAL = 25 marks]

TABLE B.12 CRITICAL VALUES OF THE KRUSKAL-WALLIS H DISTRIBUTION

[illegible]

TABLE B.12 (cont.) CRITICAL VALUES OF THE POLYMER WILCOX TEST

1		2		3		4		5		6		7		8		9		10		11		12		13		14		15		16		17		18		19		20		21		22		23		24		25		26		27		28		29		30		31		32		33		34		35		36		37		38		39		40		41		42		43		44		45		46		47		48		49		50		51		52		53		54		55		56		57		58		59		60		61		62		63		64		65		66		67		68		69		70		71		72		73		74		75		76		77		78		79		80		81		82		83		84		85		86		87		88		89		90		91		92		93		94		95		96		97		98		99		100		101		102		103		104		105		106		107		108		109		110		111		112		113		114		115		116		117		118		119		120		121		122		123		124		125		126		127		128		129		130		131		132		133		134		135		136		137		138		139		140		141		142		143		144		145		146		147		148		149		150		151		152		153		154		155		156		157		158		159		160		161		162		163		164		165		166		167		168		169		170		171		172		173		174		175		176		177		178		179		180		181		182		183		184		185		186		187		188		189		190		191		192		193		194		195		196		197		198		199		200		201		202		203		204		205		206		207		208		209		210		211		212		213		214		215		216		217		218		219		220		221		222		223		224		225		226		227		228		229		230		231		232		233		234		235		236		237		238		239		240		241		242		243		244		245		246		247		248		249		250		251		252		253		254		255		256		257		258		259		260		261		262		263		264		265		266		267		268		269		270		271		272		273		274		275		276		277		278		279		280		281		282		283		284		285		286		287		288		289		290		291		292		293		294		295		296		297		298		299		300		301		302		303		304		305		306		307		308		309		310		311		312		313		314		315		316		317		318		319		320		321		322		323		324		325		326		327		328		329		330		331		332		333		334		335		336		337		338		339		340		341		342		343		344		345		346		347		348		349		350		351		352		353		354		355		356		357		358		359		360		361		362		363		364		365		366		367		368		369		370		371		372		373		374		375		376		377		378		379		380		381		382		383		384		385		386		387		388		389		390		391		392		393		394		395		396		397		398		399		400		401		402		403		404		405		406		407		408		409		410		411		412		413		414		415		416		417		418		419		420		421		422		423		424		425		426		427		428		429		430		431		432		433		434		435		436		437		438		439		440		441		442		443		444		445		446		447		448		449		450		451		452		453		454		455		456		457		458		459		460		461		462		463		464		465		466		467		468		469		470		471		472		473		474		475		476		477		478		479		480		481		482		483		484		485		486		487		488		489		490		491		492		493		494		495		496		497		498		499		500		501		502		503		504		505		506		507		508		509		510		511		512		513		514		515		516		517		518		519		520		521		522		523		524		525		526		527		528		529		530		531		532		533		534		535		536		537		538		539		540		541		542		543		544		545		546		547		548		549		550		551		552		553		554		555		556		557		558		559		560		561		562		563		564		565		566		567		568		569		570		571		572		573		574		575		576		577		578		579		580		581		582		583		584		585		586		587		588		589		590		591		592		593		594		595		596		597		598		599		600		601		602		603		604		605		606		607		608		609		610		611		612		613		614		615		616		617		618		619		620		621		622		623		624		625		626		627		628		629		630		631		632		633		634		635		636		637		638		639		640		641		642		643		644		645		646		647		648		649		650		651		652		653		654		655		656		657		658		659		660		661		662		663		664		665		666		667		668		669		670		671		672		673		674		675		676		677		678		679		680		681		682		683		684		685		686		687		688		689		690		691		692		693		694		695		696		697		698		699		700		701		702		703		704		705		706		707		708		709		710		711		712		713		714		715		716		717		718		719		720		721		722		723		724		725		726		727		728		729		730		731		732		733		734		735		736		737		738		739		740		741		742		743		744		745		746		747		748		749		750		751		752		753		754		755		756		757		758		759		760		761		762		763		764		765		766		767		768		769		770		771		772		773		774		775		776		777		778		779		780		781		782		783		784		785		786		787		788		789		790		791		792		793		794		795		796		797		798		799		800		801		802		803		804		805		806		807		808		809		810		811		812		813		814		815		816		817		818		819		820		821		822		823		824		825		826		827		828		829		830		831		832		833		834		835		836		837		838		839		840		841		842		843		844		845		846		847		848		849		850		851		852		853		854		855		856		857		858		859		860		861		862		863		864		865		866		867		868		869		870		871		872		873		874		875		876		877		878		879		880		881		882		883		884		885		886		887		888		889		890		891		892		893		894		895		896		897		898		899		900		901		902		903		904		905		906		907		908		909		910		911		912		913		914		915		916		917		918		919		920		921		922		923		924		925		926		927		928		929		930		931		932		933		934		935		936		937		938		939		940		941		942		943		944		945		946		947		948		949		950		951		952		953		954		955		956		957		958		959		960		961		962		963		964		965		966		967		968		969		970		971		972		973		974		975		976		977		978		979		980		981		982		983		984		985		986		987		988		989		990		991		992		993		994		995		996		997		998		999		1000		1001		1002		1003		1004		1005		1006		1007		1008		1009		1010		1011		1012		1013		1014		1015		1016		1017		1018	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Example 1:

$$H_{0.05,4,3,2} = 5.444 \text{ and } H_{0.01,4,4,3} = H_{0.01,4,4,4} = 7.769$$

TABLE B.4 CRITICAL VALUES OF THE F DISTRIBUTION

		Numerator DF = 1								
		$\alpha(2):$	0.30	0.20	0.10	0.05	0.02	0.01	0.005	0.002
Denom. DF		$\alpha(1):$	0.30	0.20	0.10	0.05	0.02	0.01	0.005	0.001
			0.30	0.20	0.10	0.05	0.02	0.01	0.005	0.0005
1			5.02	4.00	3.00	2.16	1.58	1.10	0.85	0.64
2			4.10	3.00	2.00	1.43	1.05	0.71	0.54	0.41
3			3.78	2.75	1.77	1.30	0.94	0.64	0.49	0.37
4			3.59	2.58	1.61	1.20	0.86	0.59	0.45	0.34
5			3.46	2.46	1.50	1.12	0.80	0.54	0.41	0.31
6			3.36	2.37	1.42	1.06	0.76	0.51	0.39	0.29
7			3.28	2.30	1.36	1.01	0.72	0.48	0.37	0.27
8			3.21	2.24	1.31	0.97	0.69	0.46	0.35	0.25
9			3.15	2.19	1.27	0.93	0.66	0.44	0.33	0.24
10			3.10	2.15	1.24	0.90	0.64	0.42	0.31	0.22
11			3.06	2.11	1.21	0.88	0.62	0.41	0.30	0.21
12			3.02	2.08	1.18	0.86	0.60	0.40	0.29	0.20
13			2.99	2.05	1.16	0.84	0.58	0.39	0.28	0.19
14			2.96	2.03	1.14	0.83	0.57	0.38	0.27	0.18
15			2.94	2.01	1.12	0.82	0.56	0.37	0.26	0.17
16			2.92	1.99	1.10	0.81	0.55	0.36	0.25	0.16
17			2.90	1.97	1.08	0.80	0.54	0.35	0.24	0.15
18			2.88	1.95	1.06	0.79	0.53	0.34	0.23	0.14
19			2.86	1.93	1.04	0.78	0.52	0.33	0.22	0.13
20			2.84	1.91	1.02	0.77	0.51	0.32	0.21	0.12
21			2.82	1.89	1.00	0.76	0.50	0.31	0.20	0.11
22			2.80	1.87	0.98	0.75	0.49	0.30	0.19	0.10
23			2.78	1.85	0.96	0.74	0.48	0.29	0.18	0.09
24			2.76	1.83	0.94	0.73	0.47	0.28	0.17	0.08
25			2.74	1.81	0.92	0.72	0.46	0.27	0.16	0.07
26			2.72	1.79	0.90	0.71	0.45	0.26	0.15	0.06
27			2.70	1.77	0.88	0.70	0.44	0.25	0.14	0.05
28			2.68	1.75	0.86	0.69	0.43	0.24	0.13	0.04
29			2.66	1.73	0.84	0.68	0.42	0.23	0.12	0.03
30			2.64	1.71	0.82	0.67	0.41	0.22	0.11	0.02
35			2.57	1.65	0.78	0.64	0.40	0.21	0.10	0.01
40			2.51	1.59	0.74	0.61	0.38	0.20	0.09	0.00
45			2.46	1.54	0.70	0.58	0.36	0.19	0.08	0.00
50			2.41	1.49	0.66	0.55	0.34	0.18	0.07	0.00
55			2.37	1.45	0.63	0.52	0.32	0.17	0.06	0.00
60			2.33	1.41	0.60	0.50	0.31	0.16	0.05	0.00
65			2.30	1.38	0.58	0.48	0.30	0.15	0.04	0.00
70			2.27	1.35	0.56	0.46	0.29	0.14	0.03	0.00
80			2.22	1.30	0.52	0.43	0.27	0.13	0.02	0.00
90			2.18	1.26	0.49	0.40	0.25	0.12	0.01	0.00
100			2.15	1.23	0.47	0.38	0.24	0.11	0.00	0.00
120			2.10	1.18	0.43	0.35	0.22	0.10	0.00	0.00
140			2.06	1.14	0.40	0.32	0.20	0.09	0.00	0.00
160			2.03	1.11	0.38	0.30	0.19	0.08	0.00	0.00
180			2.00	1.08	0.36	0.28	0.18	0.07	0.00	0.00
200			1.98	1.06	0.35	0.27	0.17	0.06	0.00	0.00
250			1.93	1.01	0.32	0.24	0.15	0.05	0.00	0.00
300			1.89	0.97	0.30	0.22	0.14	0.04	0.00	0.00
400			1.83	0.91	0.26	0.19	0.12	0.03	0.00	0.00
500			1.78	0.86	0.23	0.17	0.11	0.02	0.00	0.00
-			1.74	0.82	0.21	0.15	0.10	0.01	0.00	0.00

TABLE B.1 CRITICAL VALUES OF THE CHI-SQUARE DISTRIBUTION

ν	$\alpha = 0.999$	0.995	0.99	0.975	0.95	0.90	0.75	0.50	0.25	0.10	0.05	0.025	0.01	0.005	0.001
1	0.000	0.000	0.000	0.001	0.004	0.016	0.102	0.455	1.125	2.706	3.841	5.024	6.635	7.879	10.828
2	0.002	0.010	0.020	0.051	0.103	0.211	0.575	1.386	2.773	4.605	5.991	7.378	9.210	10.597	13.838
3	0.024	0.072	0.115	0.216	0.352	0.584	1.213	2.366	4.108	6.251	7.815	9.348	11.345	12.838	16.276
4	0.091	0.207	0.297	0.484	0.711	1.064	1.865	2.357	5.385	7.779	9.488	11.143	13.277	14.860	18.467
5	0.210	0.412	0.554	0.831	1.145	1.610	2.675	4.351	6.626	9.236	11.070	12.833	15.086	16.750	20.515
6	0.381	0.676	0.872	1.237	1.635	2.204	3.455	5.348	7.881	10.645	12.592	14.449	16.812	18.548	22.458
7	0.589	0.888	1.124	1.690	2.167	2.833	4.255	6.346	9.037	12.017	14.067	16.013	18.475	20.278	24.332
8	0.857	1.356	1.646	2.180	2.713	3.490	5.071	7.344	10.219	13.362	15.507	17.535	20.090	21.955	26.194
9	1.152	1.735	2.008	2.700	3.325	4.168	5.891	8.143	11.591	14.684	16.919	19.023	21.666	23.589	27.877
10	1.479	2.156	2.558	3.247	3.940	4.865	6.757	9.342	12.549	15.987	18.307	20.483	23.103	25.188	29.588
11	1.834	2.603	3.053	3.816	4.575	5.578	7.884	10.341	13.701	17.275	19.675	21.920	24.725	26.757	31.264
12	2.214	3.054	3.571	4.404	5.225	6.304	9.238	11.540	14.645	18.583	21.026	23.537	26.217	28.306	32.909
13	2.601	3.505	4.107	5.009	5.882	7.042	10.259	12.549	15.684	19.682	22.362	24.736	27.688	29.819	34.524
14	3.001	4.036	4.680	5.684	6.571	7.790	11.155	13.733	16.917	21.064	23.685	26.119	29.141	31.319	36.123
15	3.443	4.601	5.239	6.368	7.261	8.547	12.157	14.939	18.245	22.307	24.996	27.488	30.578	32.801	37.697
16	3.942	5.192	5.812	6.968	7.962	9.312	13.272	16.158	19.369	23.542	26.295	28.845	31.991	34.267	39.252
17	4.448	5.697	6.408	7.564	8.672	10.085	14.452	17.338	20.483	24.769	27.587	30.191	33.409	35.718	40.790
18	4.983	6.205	7.015	8.153	9.390	10.851	15.852	18.538	21.605	25.989	28.869	31.526	34.805	37.156	42.324
19	5.541	6.744	7.633	8.707	10.117	11.651	17.151	19.732	22.778	27.204	30.144	32.852	36.191	38.582	43.820
20	6.121	7.314	8.280	9.391	10.931	12.443	18.552	21.337	23.928	28.448	31.410	34.170	37.566	39.997	45.315
21	6.724	7.914	8.897	10.083	11.591	13.240	19.544	22.337	24.935	29.635	32.671	35.479	38.932	41.401	46.797
22	7.359	8.545	9.542	10.802	12.538	14.041	20.780	23.587	26.039	30.843	33.924	36.784	40.289	42.786	48.268
23	8.028	9.208	10.219	11.563	13.681	14.843	22.137	24.737	27.141	32.047	35.172	38.078	41.401	44.181	49.681
24	8.743	9.920	10.955	12.401	14.648	15.645	23.587	25.937	28.241	33.187	36.415	39.344	42.659	45.550	51.179
25	9.506	10.680	11.724	13.240	15.511	16.447	25.000	26.833	29.288	34.382	37.652	40.646	43.824	46.928	52.620
26	9.983	11.160	12.198	13.844	15.379	17.249	26.183	27.983	30.435	35.563	38.885	41.923	45.042	48.290	54.052
27	10.495	11.678	12.679	14.373	16.151	18.118	27.483	28.938	31.573	36.781	40.113	43.185	46.183	49.645	55.486
28	10.986	12.181	13.155	14.861	16.928	18.988	28.957	29.937	32.620	37.916	41.337	44.347	47.349	50.993	56.892
29	11.508	12.707	13.655	15.385	17.798	19.798	30.587	30.939	33.711	39.087	42.557	45.504	48.500	52.156	58.301
30	12.042	13.247	14.183	15.935	18.593	20.559	31.776	31.937	34.808	40.286	43.773	46.666	49.666	53.672	59.703
31	12.588	13.800	14.738	16.515	19.421	21.360	32.984	32.937	35.847	41.482	44.985	47.823	50.823	54.932	61.098
32	13.146	14.368	15.298	17.119	20.272	22.187	34.000	33.937	36.885	42.653	46.154	48.979	51.979	56.183	62.487
33	13.715	14.951	15.882	17.744	21.147	23.038	35.033	34.937	37.944	43.834	47.337	50.125	53.125	57.443	63.879
34	14.295	15.548	16.485	18.391	22.043	23.918	36.087	35.937	39.028	44.985	48.523	51.272	54.272	58.694	65.267
35	14.886	16.158	17.107	19.061	22.964	24.825	37.159	36.937	40.141	46.087	49.723	52.423	55.423	60.000	66.649
36	15.488	16.781	17.744	19.764	23.909	25.758	38.287	37.937	41.288	47.187	50.885	53.572	56.572	61.293	67.995
37	16.101	17.417	18.401	20.499	24.878	26.708	39.433	38.937	42.468	48.287	51.985	54.722	57.722	62.578	69.385
38	16.724	18.066	19.078	21.276	25.881	27.687	40.597	39.937	43.681	49.387	53.187	55.872	58.872	63.853	70.769
39	17.357	18.728	19.774	22.087	26.906	28.698	41.778	40.937	44.918	50.487	54.418	57.022	60.022	65.033	72.147
40	17.999	19.401	20.491	22.921	27.954	29.741	42.987	41.937	46.087	51.587	55.618	58.172	61.172	66.203	73.519
41	18.650	20.086	21.216	23.787	28.933	30.816	44.000	42.937	47.187	52.687	56.818	59.322	62.322	67.363	74.885
42	19.310	20.783	21.961	24.684	29.944	31.831	45.033	43.937	48.287	53.787	57.963	60.472	63.472	68.513	76.243
43	19.979	21.491	22.726	25.611	30.986	32.831	46.087	44.937	49.387	54.887	59.113	61.622	64.622	69.663	77.595
44	20.657	22.210	23.509	26.568	32.167	33.816	47.159	45.937	50.487	55.987	60.263	62.772	65.772	70.813	78.941
45	21.344	22.941	24.310	27.544	33.533	34.787	48.244	46.937	51.587	57.087	61.413	63.922	66.922	71.963	80.077
46	22.039	23.683	25.129	28.539	34.833	35.741	49.344	47.937	52.687	58.187	62.563	65.072	68.072	73.103	81.203
47	22.742	24.436	25.956	29.554	36.167	36.687	50.459	48.937	53.787	59.287	63.713	66.222	69.222	74.233	82.323
48	23.452	25.199	26.791	30.589	37.533	37.622	51.587	49.937	54.887	60.387	64.863	67.372	70.372	75.363	83.443
49	24.169	25.972	27.633	31.638	38.401	38.547	52.687	50.937	55.987	61.487	65.987	68.522	71.522	76.493	84.563
50	24.893	26.755	28.484	32.703	39.287	39.451	53.787	51.937	57.087	62.587	67.137	69.672	72.672	77.623	85.683

TABLE B.3 (cont.) CRITICAL VALUES OF THE F DISTRIBUTION

Numerator df = 1		Denominator df									
		1	2	3	4	5	6	7	8	9	10
1	161.448	161.448	159.923	158.583	157.317	156.116	154.971	153.873	152.815	151.790	150.793
2	19.1644	19.1644	18.9872	18.8207	18.6639	18.5158	18.3755	18.2421	18.1148	17.9920	17.8732
3	10.1280	10.1280	10.0000	9.8868	9.7779	9.6730	9.5719	9.4744	9.3803	9.2894	9.2015
4	7.70854	7.70854	7.60000	7.50000	7.40449	7.31249	7.22389	7.13859	7.05649	6.97749	6.90149
5	6.59126	6.59126	6.49000	6.39375	6.29940	6.20684	6.11597	6.02669	5.93890	5.85250	5.76839
6	5.96456	5.96456	5.87000	5.77500	5.68040	5.58714	5.49512	5.40424	5.31440	5.22550	5.13844
7	5.59126	5.59126	5.50000	5.40625	5.31190	5.21894	5.12727	5.03679	4.94740	4.85900	4.77249
8	5.31838	5.31838	5.23000	5.13375	5.03740	4.94194	4.84727	4.75329	4.65990	4.56710	4.47579
9	5.11838	5.11838	5.03000	4.93375	4.83740	4.74194	4.64727	4.55329	4.45990	4.36710	4.27579
10	4.96838	4.96838	4.88000	4.78375	4.68740	4.59194	4.49727	4.40329	4.30990	4.21710	4.12579
15	4.45838	4.45838	4.37000	4.27375	4.17740	4.08194	3.98727	3.89329	3.79990	3.70710	3.61579
20	4.17838	4.17838	4.09000	4.00000	3.90449	3.80940	3.71494	3.62127	3.52840	3.43640	3.34579
30	3.94838	3.94838	3.86000	3.77000	3.67449	3.57940	3.48494	3.39127	3.29840	3.20640	3.11579
40	3.80838	3.80838	3.72000	3.63000	3.53449	3.43940	3.34494	3.25127	3.15840	3.06640	2.97579
50	3.70838	3.70838	3.62000	3.53000	3.43449	3.33940	3.24494	3.15127	3.05840	2.96640	2.87579
60	3.63838	3.63838	3.55000	3.46000	3.36449	3.26940	3.17494	3.08127	2.98840	2.89640	2.80579
70	3.58838	3.58838	3.50000	3.41000	3.31449	3.21940	3.12494	3.03127	2.93840	2.84640	2.75579
80	3.54838	3.54838	3.46000	3.37000	3.27449	3.17940	3.08494	2.99127	2.89840	2.80640	2.71579
90	3.51838	3.51838	3.43000	3.34000	3.24449	3.14940	3.05494	2.96127	2.86840	2.77640	2.68579
100	3.49838	3.49838	3.41000	3.32000	3.22449	3.12940	3.03494	2.94127	2.84840	2.75640	2.66579

TABLE B.4 (cont.) CRITICAL VALUES OF THE F DISTRIBUTION

Numerator df = 1		Denominator df									
		1	2	3	4	5	6	7	8	9	10
1	161.448	161.448	159.923	158.583	157.317	156.116	154.971	153.873	152.815	151.790	150.793
2	19.1644	19.1644	18.9872	18.8207	18.6639	18.5158	18.3755	18.2421	18.1148	17.9920	17.8732
3	10.1280	10.1280	10.0000	9.8868	9.7779	9.6730	9.5719	9.4744	9.3803	9.2894	9.2015
4	7.70854	7.70854	7.60000	7.50000	7.40449	7.31249	7.22389	7.13859	7.05649	6.97749	6.90149
5	6.59126	6.59126	6.49000	6.39375	6.29940	6.20684	6.11597	6.02669	5.93890	5.85250	5.76839
6	5.96456	5.96456	5.87000	5.77500	5.68040	5.58714	5.49512	5.40424	5.31440	5.22550	5.13844
7	5.59126	5.59126	5.50000	5.40625	5.31190	5.21894	5.12727	5.03679	4.94740	4.85900	4.77249
8	5.31838	5.31838	5.23000	5.13375	5.03740	4.94194	4.84727	4.75329	4.65990	4.56710	4.47579
9	5.11838	5.11838	5.03000	4.93375	4.83740	4.74194	4.64727	4.55329	4.45990	4.36710	4.27579
10	4.96838	4.96838	4.88000	4.78375	4.68740	4.59194	4.49727	4.40329	4.30990	4.21710	4.12579
15	4.45838	4.45838	4.37000	4.27375	4.17740	4.08194	3.98727	3.89329	3.79990	3.70710	3.61579
20	4.17838	4.17838	4.09000	4.00000	3.90449	3.80940	3.71494	3.62127	3.52840	3.43640	3.34579
30	3.94838	3.94838	3.86000	3.77000	3.67449	3.57940	3.48494	3.39127	3.29840	3.20640	3.11579
40	3.80838	3.80838	3.72000	3.63000	3.53449	3.43940	3.34494	3.25127	3.15840	3.06640	2.97579
50	3.70838	3.70838	3.62000	3.53000	3.43449	3.33940	3.24494	3.15127	3.05840	2.96640	2.87579
60	3.63838	3.63838	3.55000	3.46000	3.36449	3.26940	3.17494	3.08127	2.98840	2.89640	2.80579
70	3.58838	3.58838	3.50000	3.41000	3.31449	3.21940	3.12494	3.03127	2.93840	2.84640	2.75579
80	3.54838	3.54838	3.46000	3.37000	3.27449	3.17940	3.08494	2.99127	2.89840	2.80640	2.71579
90	3.51838	3.51838	3.43000	3.34000	3.24449	3.14940	3.05494	2.96127	2.86840	2.77640	2.68579
100	3.49838	3.49838	3.41000	3.32000	3.22449	3.12940	3.03494	2.94127	2.84840	2.75640	2.66579

TABLE B.5 (cont.) CRITICAL VALUES OF THE F DISTRIBUTION

Numerator df = 1		Denominator df									
		1	2	3	4	5	6	7	8	9	10
1	161.448	161.448	159.923	158.583	157.317	156.116	154.971	153.873	152.815	151.790	150.793
2	19.1644	19.1644	18.9872	18.8207	18.6639	18.5158	18.3755	18.2421	18.1148	17.9920	17.8732
3	10.1280	10.1280	10.0000	9.8868	9.7779	9.6730	9.5719	9.4744	9.3803	9.2894	9.2015
4	7.70854	7.70854	7.60000	7.50000	7.40449	7.31249	7.22389	7.13859	7.05649	6.97749	6.90149
5	6.59126	6.59126	6.49000	6.39375	6.29940	6.20684	6.11597	6.02669	5.93890	5.85250	5.76839
6	5.96456	5.96456	5.87000	5.77500	5.68040	5.58714	5.49512	5.40424	5.31440	5.22550	5.13844
7	5.59126	5.59126	5.50000	5.40625	5.31190	5.21894	5.12727	5.03679	4.94740	4.85900	4.77249
8	5.31838	5.31838	5.23000	5.13375	5.03740	4.94194	4.84727	4.75329	4.65990	4.56710	4.47579
9	5.11838	5.11838	5.03000	4.93375	4.83740	4.74194	4.64727	4.55329	4.45990	4.36710	4.27579
10	4.96838	4.96838	4.88000	4.78375	4.68740	4.59194	4.49727	4.40329	4.30990	4.21710	4.12579
15	4.45838	4.45838	4.37000	4.27375	4.17740	4.08194	3.98727	3.89329	3.79990	3.70710	3.61579
20	4.17838	4.17838	4.09000	4.00000	3.90449	3.80940	3.71494	3.62127	3.52840	3.43640	3.34579
30	3.94838	3.94838	3.86000	3.77000	3.67449	3.57940	3.48494	3.39127	3.29840	3.20640	3.11579
40	3.80838	3.80838	3.72000	3.63000	3.53449	3.43940	3.34494	3.25127	3.15840	3.06640	2.97579
50	3.70838	3.70838	3.62000	3.53000	3.43449	3.33940	3.24494	3.15127	3.05840	2.96640	2.87579
60	3.63838	3.63838	3.55000	3.46000	3.36449	3.26940	3.17494	3.08127	2.98840	2.89640	2.80579
70	3.58838	3.58838	3.50000	3.41000	3.31449	3.21940	3.12494	3.03127	2.93840	2.84640	2.75579
80	3.54838	3.54838	3.46000	3.37000	3.27449	3.17940	3.08494	2.99127	2.89840	2.80640	2.71579
90	3.51838	3.51838	3.43000	3.34000	3.24449	3.14940	3.05494	2.96127	2.86840	2.77640	2.68579
100	3.49838	3.49838	3.41000	3.32000	3.22449	3.12940	3.03494	2.94127	2.84840	2.75640	2.66579